

1 GCM-Filters: A Python Package for Diffusion-based 2 Spatial Filtering of Gridded Data

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13 Summary

14 GCM-Filters is a python package that allows scientists to perform spatial filtering analysis
15 in an easy, flexible and efficient way. The package implements the filtering method based on
16 the discrete Laplacian operator that was introduced by Grooms et al. (2021). The filtering
17 algorithm is analogous to smoothing via diffusion; hence the name *diffusion-based filters*.
18 GCM-Filters can be used with either gridded observational data or gridded data that is
19 produced by General Circulation Models (GCMs) of ocean, weather, and climate. Spatial
20 filtering of observational or GCM data is a common analysis method in the Earth Sciences,
21 for example to study oceanic and atmospheric motions at different spatial scales or to develop
22 subgrid-scale parameterizations for ocean models.

23 GCM-Filters provides filters that are highly configurable, with the goal to be useful for a wide
24 range of scientific applications. The user has different options for selecting the filter scale and
25 filter shape. The filter scale can be defined in several ways: a fixed length scale (e.g., 100
26 km), a scale tied to a model grid scale (e.g., 1°), or a scale tied to a varying dynamical scale
27 (e.g., the Rossby radius of deformation). As an example, [Figure 1](#) shows unfiltered and filtered
28 relative vorticity, where the filter scale is set to a model grid scale of 4° . GCM-Filters also
29 allows for anisotropic, i.e., direction-dependent, filtering. Finally, the filter shape – currently:
30 either Gaussian or Taper – determines how sharply the filter separates scales above and below
31 the target filter scale.

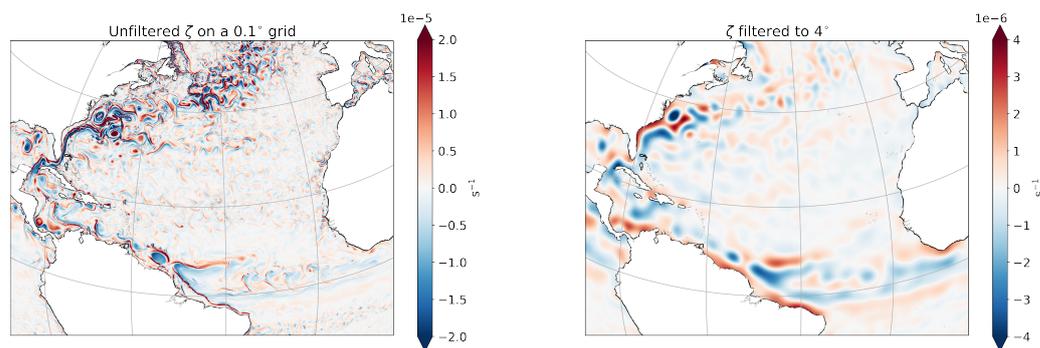


Figure 1: (Left) Snapshot of unfiltered surface relative vorticity $\zeta = \partial_x v - \partial_y u$ from a global 0.1° simulation with MOM6 (Adcroft et al., 2019). (Right) Relative vorticity filtered to 4° , obtained by applying GCM-Filters to the field ζ on the left. The plots are made with matplotlib (Hunter, 2007) and cartopy (Met Office, 2010 - 2015).

Statement of Need

Spatial filtering is commonly used as a scientific tool for analyzing gridded data. An example of an existing spatial filtering tool in python is SciPy's (Virtanen et al., 2020) `ndimage.gaussian_filter` function, implemented as a sequence of convolution filters. While being a valuable tool for image processing (or blurring), SciPy's Gaussian filter is of limited use for GCM data; it assumes a regular and rectangular Cartesian grid, employs a simple boundary condition, and the definitions of filter scale and shape have little or no flexibility. The python package GCM-Filters is specifically designed to filter GCM data, and seeks to solve a number of challenges for the user:

1. GCM data comes on irregular curvilinear grids with spatially varying grid-cell geometry.
2. Continental boundaries require careful and special treatment when filtering ocean GCM output.
3. Earth Science applications benefit from configurable filters, where the definition of filter scale and shape is flexible.
4. GCM output is often too large to process in memory, requiring distributed and / or delayed execution.

The GCM-Filters algorithm (Grooms et al., 2021) applies a discrete Laplacian to smooth a field through an iterative process that resembles diffusion. The discrete Laplacian takes into account the varying grid-cell geometry and uses a no-flux boundary condition, mimicking how diffusion is internally implemented in GCMs. The no-flux boundary conditions ensures that the filter preserves the integral: $\int_{\Omega} \bar{f}(x, y) dA = \int_{\Omega} f(x, y) dA$, where f is the original field, \bar{f} the filtered field, and Ω the ocean domain. Conservation of the integral is a desirable filter property for many physical quantities, for example energy or ocean salinity. More details on the filter properties can be found in Grooms et al. (2021).

An important goal of GCM-Filters is to enable computationally efficient filtering. The user can employ GCM-Filters on either CPUs or GPUs, with NumPy (Harris et al., 2020) or CuPy (Okuta et al., 2017) input data. GCM-Filters leverages Dask (Dask Development Team, 2016) and Xarray (Hoyer & Hamman, 2017) to support filtering of larger-than-memory datasets and computational flexibility.

61 Usage

62 The main GCM-`Filters` class that the user will interface with is the `gcm_filters.Filter`
63 object. When creating a filter object, the user specifies how they want to smooth their data,
64 including the desired filter shape and filter scale. At this stage, the user also picks the grid
65 type that matches their GCM data, given a predefined list of grid types. Each grid type
66 has an associated discrete Laplacian, and requires different *grid variables* that the user must
67 provide (the latter are usually available to the user as part of the GCM output). Currently,
68 GCM-`Filters` provides a number of different grid types and associated discrete Laplacians:

- 69 ■ Grid types with **scalar Laplacians** that can be used for filtering scalar fields, for example
70 temperature or vorticity (see [Figure 1](#)). The currently implemented grid types are
71 compatible with different ocean GCM grids including MOM5 (MOM 5 Development
72 Team, 2012), MOM6 (Adcroft et al., 2019) and the POP2 (Smith et al., 2010) tripole
73 grid.
- 74 ■ Grid types with **vector Laplacians** that can be used for filtering vector fields, for example
75 horizontal velocity (u, v) . The currently implemented grid type is compatible with ocean
76 GCM grids that use an Arakawa C-grid convention; examples include MOM6 (Adcroft
77 et al., 2019) and the MITgcm (Campin et al., 2021).

78 Atmospheric model grids are not yet supported, but could be implemented within the GCM-`F`
79 `ilters` package. Users are encouraged to contribute more grid types and Laplacians via pull
80 requests. While we are excited to share GCM-`Filters` in its current beta state at version 0.1.3,
81 we plan to continue improving and maintaining the package for the long run and welcome
82 new contributors from the broader community.

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