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# **SPAMS Documentation**

*Release 1*

**jp**

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Contents:

<code>sort(X[, mode])</code>	sort the elements of X using quicksort
<code>calcAAt(A)</code>	Compute efficiently $AA^t = A \cdot A'$ , when A is sparse and has a lot more columns than rows.
<code>calcXAt(X, A)</code>	Compute efficiently $XAt = X \cdot A'$ , when A is sparse and has a lot more columns than rows.
<code>calcXY(X, Y)</code>	Compute $Z=XY$ using the BLAS library used by SPAMS.
<code>calcXYt(X, Y)</code>	Compute $Z=XY'$ using the BLAS library used by SPAMS.
<code>calcXtY(X, Y)</code>	Compute $Z=X'Y$ using the BLAS library used by SPAMS.
<code>bayer(X, offset)</code>	bayer applies a Bayer pattern to an image X.
<code>conjGrad(A, b[, x0, tol, itermax])</code>	Conjugate gradient algorithm, sometimes faster than the equivalent python function solve.
<code>invSym(A)</code>	returns the inverse of a symmetric matrix A
<code>normalize(A)</code>	rescale the columns of X so that they have unit l2-norm.
<code>sparseProject(U[, thrs, mode, lambda1, ...])</code>	sparseProject solves various optimization problems, including projections on a few convex sets.
<code>lasso(X[, D, Q, q, return_reg_path, L, ...])</code>	lasso is an efficient implementation of the homotopy-LARS algorithm for solving the Lasso.
<code>lassoMask(X, D, B[, L, lambda1, lambda2, ...])</code>	lasso is a variant of lasso that handles binary masks.
<code>lassoWeighted(X, D, W[, L, lambda1, mode, ...])</code>	lassoWeighted is an efficient implementation of the LARS algorithm for solving the weighted Lasso.
<code>omp(X, D[, L, eps, lambda1, ...])</code>	omp is an efficient implementation of the Orthogonal Matching Pursuit algorithm.
<code>ompMask(X, D, B[, L, eps, lambda1, ...])</code>	ompMask is a variant of omp that allow using a binary mask B

Continued on next page

Table 1 – continued from previous page

<code>cd(X, D, A0[, lambda1, mode, itermax, tol, ...])</code>	cd addresses l1-decomposition problem with a coordinate descent type of approach.
<code>somp(X, D, list_groups[, L, eps, numThreads])</code>	somp is an efficient implementation of a Simultaneous Orthogonal Matching Pursuit algorithm.
<code>l1L2BCD(X, D, alpha0, list_groups[, ...])</code>	l1L2BCD is a solver for a Simultaneous signal decomposition formulation based on block coordinate descent.
<code>fistaFlat(Y, X, W0[, return_optim_info, ...])</code>	fistaFlat solves sparse regularized problems.
<code>fistaTree(Y, X, W0, tree[, ...])</code>	fistaTree solves sparse regularized problems.
<code>fistaGraph(Y, X, W0, graph[, ...])</code>	fistaGraph solves sparse regularized problems.
<code>proximalFlat(U[, return_val_loss, ...])</code>	proximalFlat computes proximal operators.
<code>proximalTree(U, tree[, return_val_loss, ...])</code>	proximalTree computes a proximal operator.
<code>proximalGraph(U, graph[, return_val_loss, ...])</code>	proximalGraph computes a proximal operator.
<code>trainDL(X[, return_model, model, D, ...])</code>	trainDL is an efficient implementation of the dictionary learning technique presented in
<code>structTrainDL(X[, return_model, model, D, ...])</code>	structTrainDL is an efficient implementation of the dictionary learning technique presented in
<code>trainDL_Memory(X[, D, numThreads, ...])</code>	trainDL_Memory is an efficient but memory consuming variant of the dictionary learning technique presented in
<code>nmf(X[, return_lasso, model, numThreads, ...])</code>	trainDL is an efficient implementation of the non-negative matrix factorization technique presented in
<code>nnsC(X[, return_lasso, model, lambda1, ...])</code>	trainDL is an efficient implementation of the non-negative sparse coding technique presented in
<code>archetypalAnalysis(X[, p, Z0, returnAB, ...])</code>	documentation to appear soon
<code>decompSimplex(X, Z[, computeXtX, numThreads])</code>	documentation to appear soon
<code>simpleGroupTree(degrees)</code>	makes a structure representing a tree given the degree of each level.
<code>readGroupStruct(file)</code>	reads a text file describing “simply” the structure of groups of variables needed by proximalGraph, proximalTree, fistaGraph, fistaTree and structTrainDL and builds the corresponding group structure.
<code>groupStructOfString(s)</code>	decode a multi-line string describing “simply” the structure of groups of variables needed by proximalGraph, proximalTree, fistaGraph, fistaTree and structTrainDL and builds the corresponding group structure.
<code>graphOfGroupStruct(gstruct)</code>	converts a group structure into the graph structure used by proximalGraph, fistaGraph or structTrainDL
<code>treeOfGroupStruct(gstruct)</code>	converts a group structure into the tree structure used by proximalTree, fistaTree or structTrainDL

## SORT

`spams.sort(X, mode=True)`

sort the elements of X using quicksort

**Args:** X: double vector of size n mode: false for decreasing order (true by default)

**Returns:** Y: double vector of size n

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## CALCAAT

`spams.calcAAAt` (*A*)

Compute efficiently  $AA^t = A \cdot A'$ , when *A* is sparse

and has a lot more columns than rows. In some cases, it is up to 20 times faster than the equivalent python expression  $AA^t = A \cdot A'$ ;

**Args:** *A*: double sparse *m* x *n* matrix

**Returns:**  $AA^t$ : double *m* x *m* matrix

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## CALCXAT

`spams.calcXAt` ( $X, A$ )

Compute efficiently  $XAt = X*A'$ , when  $A$  is sparse and has a lot more columns than rows. In some cases, it is up to 20 times faster than the equivalent python expression;

**Args:**  $X$ : double  $m \times n$  matrix  $A$ : double sparse  $p \times n$  matrix

**Returns:**  $XAt$ : double  $m \times p$  matrix

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## CALCXY

`spams.calcXY` ( $X, Y$ )

Compute  $Z=XY$  using the BLAS library used by SPAMS.

**Args:**  $X$ : double  $m \times n$  matrix  $Y$ : double  $n \times p$  matrix

**Returns:**  $Z$ : double  $m \times p$  matrix

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## CALCXYT

`spams.calcXYt` ( $X, Y$ )

Compute  $Z=XY'$  using the BLAS library used by SPAMS.

**Args:**  $X$ : double  $m \times n$  matrix  $Y$ : double  $p \times n$  matrix

**Returns:**  $Z$ : double  $m \times p$  matrix

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## CALCXTY

`spams.calcXtY(X, Y)`

Compute  $Z=X'Y$  using the BLAS library used by SPAMS.

**Args:** X: double  $n \times m$  matrix Y: double  $n \times p$  matrix

**Returns:** Z: double  $m \times p$  matrix

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



**BAYER**

spams.**bayer** (*X*, *offset*)

**bayer** applies a Bayer pattern to an image **X**. There are four possible offsets.

**Args:** *X*: double  $m \times n$  matrix *offset*: scalar, 0,1,2 or 3

**Returns:** *Y*: double  $m \times m$  matrix

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## CONJGRAD

`spams.conjGrad(A, b, x0=None, tol=1e-10, itermax=None)`

Conjugate gradient algorithm, sometimes faster than the equivalent python function `solve`. In order to solve  $Ax=b$ ;

**Args:** *A*: double square  $n \times n$  matrix. **HAS TO BE POSITIVE DEFINITE** *b*: double vector of length  $n$ . *x0*: double vector of length  $n$ . (optional) initial guess. *tol*: (optional) tolerance. *itermax*: (optional) maximum number of iterations.

**Returns:** *x*: double vector of length  $n$ .

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## INVSYM

`spams.invSym(A)`

returns the inverse of a symmetric matrix  $A$

**Args:**  $A$ : double  $n \times n$  matrix

**Returns:**  $B$ : double  $n \times n$  matrix

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## NORMALIZE

`spams.normalize(A)`

**rescale the columns of X so that they have** unit l2-norm.

**Args:** X: double m x n matrix

**Returns:** Y: double m x n matrix

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## SPARSEPROJECT

`spams.sparseProject` ( $U$ ,  $thrs=1.0$ ,  $mode=1$ ,  $lambda1=0.0$ ,  $lambda2=0.0$ ,  $lambda3=0.0$ ,  $pos=0$ ,  $numThreads=-1$ )

`sparseProject` solves various optimization problems, including projections on a few convex sets.

It aims at addressing the following problems for all columns  $u$  of  $U$  in parallel

1. **when mode=1 (projection on the  $l_1$ -ball)**  $\min_v \|u-v\|_2^2$  s.t.  $\|v\|_1 \leq thrs$
2. **when mode=2**  $\min_v \|u-v\|_2^2$  s.t.  $\|v\|_2^2 + lamuda1\|v\|_1 \leq thrs$
3. **when mode=3**  $\min_v \|u-v\|_2^2$  s.t.  $\|v\|_1 + 0.5lamuda1\|v\|_2^2 \leq thrs$
4. **when mode=4**  $\min_v 0.5\|u-v\|_2^2 + lamuda1\|v\|_1$  s.t.  $\|v\|_2^2 \leq thrs$
5. **when mode=5**

$$\min_v 0.5\|u-v\|_2^2 + lamuda1\|v\|_1 + lamuda2 FL(v) + \dots \quad 0.5lamuda_3 \|v\|_2^2$$

where  $FL$  denotes a “fused lasso” regularization term.

6. **when mode=6**  $\min_v \|u-v\|_2^2$  s.t.  $lamuda1\|v\|_1 + lamuda2 FL(v) + \dots$   
 $0.5lamuda3\|v\|_2^2 \leq thrs$

When  $pos=true$  and  $mode \leq 4$ , it solves the previous problems with positivity constraints

### Args:

**U:** double  $m \times n$  matrix (input signals)  $m$  is the signal size  $n$  is the number of signals to project

**Kwargs:**  $thrs$ : (parameter)  $lambda1$ : (parameter)  $lambda2$ : (parameter)  $lambda3$ : (parameter)  $mode$ : (see above)  $pos$ : (optional, false by default)  $numThreads$ : (optional, number of threads for exploiting

multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

**Returns:**  $V$ : double  $m \times n$  matrix (output matrix)

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting



## LASSO

`spams.lasso(X, D=None, Q=None, q=None, return_reg_path=False, L=-1, lambda1=None, lambda2=0.0, mode=2, pos=False, ols=False, numThreads=-1, max_length_path=-1, verbose=False, cholesky=False)`

lasso is an efficient implementation of the homotopy-LARS algorithm for solving the Lasso.

If the function is called this way `spams.lasso(X,D = D, Q = None,...)`, it aims at addressing the following problems for all columns  $x$  of  $X$ , it computes one column  $\alpha$  of  $A$  that solves

1. when `mode=0`

$$\min_{\alpha} \|x - D\alpha\|_2^2 \text{ s.t. } \|\alpha\|_1 \leq \lambda$$

2. when `mode=1`

$$\min_{\alpha} \|\alpha\|_1 \text{ s.t. } \|x - D\alpha\|_2^2 \leq \lambda$$

3. when `mode=2`

$$\min_{\alpha} 0.5\|x - D\alpha\|_2^2 + \lambda_1\|\alpha\|_1 + 0.5\lambda_2\|\alpha\|_2^2$$

If the function is called this way `spams.lasso(X,D = None, Q = Q, q = q,...)`, it solves the above optimisation problem, when  $Q=D'D$  and  $q=D'x$ .

Possibly, when `pos=true`, it solves the previous problems with positivity constraints on the vectors  $\alpha$

### Args:

**X:** double  $m \times n$  matrix (input signals)  $m$  is the signal size  $n$  is the number of signals to decompose

**D:** double  $m \times p$  matrix (dictionary)  $p$  is the number of elements in the dictionary

**Q:**  $p \times p$  double matrix ( $Q = D'D$ ) **q:**  $p \times n$  double matrix ( $q = D'X$ ) **verbose:** verbose mode **return\_reg\_path:** if true the function will return a tuple of matrices.

**Kwargs:** **lambda1:** (parameter) **lambda2:** (optional parameter for solving the Elastic-Net)

for `mode=0` and `mode=1`, it adds a ridge on the Gram Matrix

**L:** (optional), maximum number of steps of the homotopy algorithm (can be used as a stopping criterion)

**pos:** (optional, adds non-negativity constraints on the coefficients, false by default)

**mode:** (see above, by default: 2) **numThreads:** (optional, number of threads for exploiting

multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

**cholesky:** (optional, default false), choose between Cholesky implementation or one based on the matrix inversion Lemma

**ols:** (optional, default false), perform an orthogonal projection before returning the solution.

max\_length\_path: (optional) maximum length of the path, by default 4\*p

**Returns:** A: double sparse p x n matrix (output coefficients) path: optional, returns the regularisation path for the first signal

```
A = spams.lasso(X,return_reg_path = False,...) (A,path) = spams.lasso(X,return_reg_path = True,...)
```

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting (even though the output alpha is double precision)

**Examples:**

```
import numpy as np
m = 5;n = 10;nD = 5
np.random.seed(0)
X = np.asfortranarray(np.random.normal(size=(m,n)))
X = np.asfortranarray(X / np.tile(np.sqrt((X*X).sum(axis=0)), (X.shape[0],1)))
D = np.asfortranarray(np.random.normal(size=(100,200)))
D = np.asfortranarray(D / np.tile(np.sqrt((D*D).sum(axis=0)), (D.shape[0],1)))
alpha = spams.lasso(X,D = D,return_reg_path = FALSE,lambda1 = 0.15)
```

## LASSOMASK

spams.**lassoMask** (*X, D, B, L=-1, lambda1=None, lambda2=0.0, mode=2, pos=False, numThreads=-1, verbose=False*)

lasso is a variant of lasso that handles binary masks. It aims at addressing the following problems for all columns  $x$  of  $X$ , and  $\beta$  of  $B$ , it computes one column  $\alpha$  of  $A$  that solves

1. when  $\text{mode}=0$

$$\min_{\{\alpha\}} \|\text{diag}(\beta)(x - D\alpha)\|_2^2 \text{ s.t. } \|\alpha\|_1 \leq \lambda$$

2. when  $\text{mode}=1$

$$\min_{\{\alpha\}} \|\alpha\|_1 \text{ s.t. } \|\text{diag}(\beta)(x - D\alpha)\|_2^2 \leq \lambda \|\beta\|_0 / m$$

3. when  $\text{mode}=2$

$$\min_{\{\alpha\}} 0.5 \|\text{diag}(\beta)(x - D\alpha)\|_2^2 + \lambda \|\beta\|_0 / m \|\alpha\|_1 + (\lambda^2 / 2) \|\alpha\|_2^2$$

Possibly, when  $\text{pos}=\text{true}$ , it solves the previous problems with positivity constraints on the vectors  $\alpha$

### Args:

**X:** double  $m \times n$  matrix (input signals)  $m$  is the signal size  $n$  is the number of signals to decompose

**D:** double  $m \times p$  matrix (dictionary)  $p$  is the number of elements in the dictionary

**B:** boolean  $m \times n$  matrix (mask)  $p$  is the number of elements in the dictionary

verbose: verbose mode

**Kwargs:**  $\lambda_1$ : (parameter)  $L$ : (optional, maximum number of elements of each decomposition)

**pos:** (optional, adds positivity constraints on the coefficients, false by default)

mode: (see above, by default: 2)  $\lambda_2$ : (optional parameter for solving the Elastic-Net)

for  $\text{mode}=0$  and  $\text{mode}=1$ , it adds a ridge on the Gram Matrix

**numThreads:** (optional, number of threads for exploiting multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

**Returns:** A: double sparse  $p \times n$  matrix (output coefficients)

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting (even though the output alpha is double precision)

## LASSOWEIGHTED

`spams.lassoWeighted` (*X*, *D*, *W*, *L*=-1, *lambda1*=None, *mode*=2, *pos*=False, *numThreads*=-1, *verbose*=False)

`lassoWeighted` is an efficient implementation of the LARS algorithm for solving the weighted Lasso. It is optimized for solving a large number of small or medium-sized decomposition problem (and not for a single large one).

It first computes the Gram matrix  $D'D$  and then perform a Cholesky-based OMP of the input signals in parallel. For all columns  $x$  of  $X$ , and  $w$  of  $W$ , it computes one column  $\alpha$  of  $A$  which is the solution of

1. when  $mode=0$

$$\min_{\{\alpha\}} \|x - D\alpha\|_2^2 \text{ s.t. } \|\text{diag}(w)\alpha\|_1 \leq \lambda$$

2. when  $mode=1$

$$\min_{\{\alpha\}} \|\text{diag}(w)\alpha\|_1 \text{ s.t. } \|x - D\alpha\|_2^2 \leq \lambda$$

3. when  $mode=2$

$$\min_{\{\alpha\}} 0.5\|x - D\alpha\|_2^2 + \lambda \|\text{diag}(w)\alpha\|_1$$

Possibly, when  $pos=true$ , it solves the previous problems with positivity constraints on the vectors  $\alpha$

### Args:

**X:** double  $m \times n$  matrix (input signals)  $m$  is the signal size  $n$  is the number of signals to decompose

**D:** double  $m \times p$  matrix (dictionary)  $p$  is the number of elements in the dictionary

**W:** double  $p \times n$  matrix (weights) *verbose*: *verbose* mode

**Kwargs:** *lambda1*: (parameter) *L*: (optional, maximum number of elements of each decomposition)

**pos:** (optional, adds positivity constraints on the coefficients, false by default)

*mode*: (see above, by default: 2) *numThreads*: (optional, number of threads for exploiting

multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

**Returns:** *A*: double sparse  $p \times n$  matrix (output coefficients)

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting (even though the output alpha is double precision)

## OMP

`spams.omp(X, D, L=None, eps=None, lambda1=None, return_reg_path=False, numThreads=-1)`

omp is an efficient implementation of the Orthogonal Matching Pursuit algorithm. It is optimized for solving a large number of small or medium-sized decomposition problem (and not for a single large one).

It first computes the Gram matrix  $D'D$  and then perform a Cholesky-based OMP of the input signals in parallel.  $X=[x^1, \dots, x^n]$  is a matrix of signals, and it returns a matrix  $A=[\alpha^1, \dots, \alpha^n]$  of coefficients.

**it addresses for all columns  $x$  of  $X$ ,**  $\min_{\alpha} \|\alpha\|_1$  s.t.  $\|x - D\alpha\|_2^2 \leq \text{eps}$  or  $\min_{\alpha} \|x - D\alpha\|_2^2$  s.t.  $\|\alpha\|_1 \leq L$  or  $\min_{\alpha} 0.5\|x - D\alpha\|_2^2 + \lambda_1 \|\alpha\|_1$

### Args:

**X: double  $m \times n$  matrix (input signals)**  $m$  is the signal size  $n$  is the number of signals to decompose

**D: double  $m \times p$  matrix (dictionary)**  $p$  is the number of elements in the dictionary All the columns of  $D$  should have unit-norm !

**return\_reg\_path:** if true the function will return a tuple of matrices.

### Kwargs:

**L: (optional, maximum number of elements in each decomposition,**  $\min(m,p)$  by default)

**eps: (optional, threshold on the squared l2-norm of the residual,** 0 by default

**lambda1:** (optional, penalty parameter, 0 by default **numThreads:** (optional, number of threads for exploiting

multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

### Returns:

**A: double sparse  $p \times n$  matrix (output coefficients)** **path** (optional): double dense  $p \times L$  matrix (regularization path of the first signal)  $A = \text{spams.omp}(X,D,L,\text{eps},\text{return\_reg\_path} = \text{False}, \dots)$  ( $A,\text{path} = \text{spams.omp}(X,D,L,\text{eps},\text{return\_reg\_path} = \text{True}, \dots)$ )

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting (even though the output alpha is double precision)
- Passing an int32 vector of length  $n$  to  $L$  provides a different parameter  $L$  for each input signal  $x_i$

- Passing a double vector of length  $n$  to `eps` and or `lambda1` provides a different parameter `eps` (or `lambda1`) for each input signal  $x_i$

## OMPMASK

spams . **ompMask** (*X, D, B, L=None, eps=None, lambda1=None, return\_reg\_path=False, numThreads=-1*)

ompMask is a variant of omp that allow using a binary mask B

**for all columns x of X, and columns beta of B, it computes a column**  $\alpha$  of A by addressing  $\min_{\alpha} \|\alpha\|_1$  s.t  $\|\text{diag}(\beta)(x-D\alpha)\|_2^2$

$\leq \text{eps} * \|\beta\|_1 / m$

or  $\min_{\alpha} \|\text{diag}(\beta)(x-D\alpha)\|_2^2$  s.t.  $\|\alpha\|_1 \leq L$  or  $\min_{\alpha} 0.5\|\text{diag}(\beta)(x-D\alpha)\|_2^2 + \lambda_1 \|\alpha\|_1$

### Args:

**X: double m x n matrix (input signals)** m is the signal size n is the number of signals to decompose

**D: double m x p matrix (dictionary)** p is the number of elements in the dictionary All the columns of D should have unit-norm !

**B: boolean m x n matrix (mask)** p is the number of elements in the dictionary

**return\_reg\_path:** if true the function will return a tuple of matrices.

### Kwargs:

**L: (optional, maximum number of elements in each decomposition,** min(m,p) by default)

**eps: (optional, threshold on the squared l2-norm of the residual,** 0 by default

**lambda1: (optional, penalty parameter,** 0 by default **numThreads: (optional, number of threads for exploiting**

multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

### Returns:

**A: double sparse p x n matrix (output coefficients)** path (optional): double dense p x L matrix (regularization path of the first signal)  $A = \text{spams.ompMask}(X,D,B,L,\text{eps},\text{return\_reg\_path} = \text{False},\dots)$   
 $(A,\text{path}) = \text{spams.ompMask}(X,D,B,L,\text{eps},\text{return\_reg\_path} = \text{True},\dots)$

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting (even though the output  $\alpha$  is double precision)
- Passing an int32 vector of length n to L provides a different parameter L for each input signal  $x_i$

- Passing a double vector of length  $n$  to `eps` and or `lambda1` provides a different parameter `eps` (or `lambda1`) for each input signal  $x_i$

spams . **cd** (*X, D, A0, lambda1=None, mode=2, itermax=100, tol=0.001, numThreads=-1*)

cd addresses l1-decomposition problem with a coordinate descent type of approach.

It is optimized for solving a large number of small or medium-sized decomposition problem (and not for a single large one). It first computes the Gram matrix  $D'D$ . This method is particularly well adapted when there is low correlation between the dictionary elements and when one can benefit from a warm restart. It aims at addressing the two following problems for all columns  $x$  of  $X$ , it computes a column  $\alpha$  of  $A$  such that

2. when  $mode=1$

$\min_{\alpha} \|\alpha\|_1$  s.t.  $\|x - D\alpha\|_2^2 \leq \lambda$  For this constraint setting, the method solves a sequence of penalized problems (corresponding to  $mode=2$ ) and looks for the corresponding Lagrange multiplier with a simple but efficient heuristic.

3. when  $mode=2$

$\min_{\alpha} 0.5\|x - D\alpha\|_2^2 + \lambda\|\alpha\|_1$

**Args:**

**X:** double  $m \times n$  matrix (input signals)  $m$  is the signal size  $n$  is the number of signals to decompose

**D:** double  $m \times p$  matrix (dictionary)  $p$  is the number of elements in the dictionary All the columns of  $D$  should have unit-norm !

**A0:** double sparse  $p \times n$  matrix (initial guess)

**Kwargs:**  $\lambda$ : (parameter)  $mode$ : (optional, see above, by default 2)  $itermax$ : (maximum number of iterations)  $tol$ : (tolerance parameter)  $numThreads$ : (optional, number of threads for exploiting

multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

**Returns:**  $A$ : double sparse  $p \times n$  matrix (output coefficients)

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting (even though the output  $\alpha$  is double precision)



## SOMP

`spams.somp(X, D, list_groups, L=None, eps=0.0, numThreads=-1)`

somp is an efficient implementation of a Simultaneous Orthogonal Matching Pursuit algorithm. It is optimized for solving a large number of small or medium-sized decomposition problem (and not for a single large one).

It first computes the Gram matrix  $D'D$  and then perform a Cholesky-based OMP of the input signals in parallel. It aims at addressing the following NP-hard problem

$X$  is a matrix structured in groups of signals, which we denote by  $X=[X_1, \dots, X_n]$

**for all matrices  $X_i$  of  $X$ ,**  $\min_{\{A_i\}} \|A_i\|_{\infty}$  s.t.  $\|X_i - D A_i\|_2^2 \leq \text{eps} * n_i$  where  $n_i$  is the number of columns of  $X_i$

or

$\min_{\{A_i\}} \|X_i - D A_i\|_2^2$  s.t.  $\|A_i\|_{\infty} \leq L$

### Args:

**X:** double  $m \times N$  matrix (input signals)  $m$  is the signal size  $N$  is the total number of signals

**D:** double  $m \times p$  matrix (dictionary)  $p$  is the number of elements in the dictionary All the columns of  $D$  should have unit-norm !

**list\_groups:** int32 vector containing the indices (starting at 0) of the first elements of each groups.

**Kwargs:**  $L$ : (maximum number of elements in each decomposition)  $\text{eps}$ : (threshold on the squared  $l_2$ -norm of the residual  $\text{numThreads}$ : (optional, number of threads for exploiting

multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

**Returns:** alpha: double sparse  $p \times N$  matrix (output coefficients)

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting (even though the output alpha is double precision)



## L1L2BCD

`spams.l1l2bcd(X, D, alpha0, list_groups, lambda1=None, mode=2, itermax=100, tol=0.001, numThreads=-1)`

L1L2BCD is a solver for a Simultaneous signal decomposition formulation based on block coordinate descent.

X is a matrix structured in groups of signals, which we denote by  $X=[X_1, \dots, X_n]$

**if mode=2, it solves** for all matrices  $X_i$  of X,  $\min_{\{A_i\}} 0.5\|X_i - D A_i\|_2^2 + \lambda_1 / \sqrt{n_i} \|A_i\|_{1,2}$  where  $n_i$  is the number of columns of  $X_i$

**if mode=1, it solves**  $\min_{\{A_i\}} \|A_i\|_{1,2}$  s.t.  $\|X_i - D A_i\|_2^2 \leq n_i \lambda_1$

### Args:

**X: double m x N matrix (input signals)** m is the signal size N is the total number of signals

**D: double m x p matrix (dictionary)** p is the number of elements in the dictionary

alpha0: double dense p x N matrix (initial solution) list\_groups: int32 vector containing the indices (starting at 0)

of the first elements of each groups.

**Kwargs:** lambda1: (regularization parameter) mode: (see above, by default 2) itermax: (maximum number of iterations, by default 100) tol: (tolerance parameter, by default 0.001) numThreads: (optional, number of threads for exploiting

multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

**Returns:** alpha: double sparse p x N matrix (output coefficients)

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting (even though the output alpha is double precision)



## FISTAFLAT

```
spams.fistaFlat(Y, X, W0, return_optim_info=False, numThreads=-1, max_it=1000, L0=1.0,
fixed_step=False, gamma=1.5, lambda1=1.0, delta=1.0, lambda2=0.0, lambda3=0.0,
a=1.0, b=0.0, c=1.0, tol=1e-06, it0=100, max_iter_backtracking=1000, compute_gram=False,
lin_admm=False, admm=False, intercept=False, resetflow=False, regul="", loss="",
verbose=False, pos=False, clever=False, log=False, ista=False, subgrad=False,
logName="", is_inner_weights=False, inner_weights=None, size_group=1, groups=None,
sqrt_step=True, transpose=False, linesearch_mode=0)
```

fistaFlat solves sparse regularized problems.

$X$  is a design matrix of size  $m \times p$   $X=[x^1, \dots, x^n]^T$ , where the  $x_i$ 's are the rows of  $X$   $Y=[y^1, \dots, y^n]$  is a matrix of size  $m \times n$  It implements the algorithms FISTA, ISTA and subgradient descent.

- if loss='square' and regul is a regularization function for vectors, the entries of  $Y$  are real-valued,  $W = [w^1, \dots, w^n]$  is a matrix of size  $p \times n$  For all column  $y$  of  $Y$ , it computes a column  $w$  of  $W$  such that

$$w = \operatorname{argmin} 0.5 \|y - X w\|_2^2 + \lambda \operatorname{psi}(w)$$

- if loss='square' and regul is a regularization function for matrices the entries of  $Y$  are real-valued,  $W$  is a matrix of size  $p \times n$ . It computes the matrix  $W$  such that

$$W = \operatorname{argmin} 0.5 \|Y - X W\|_F^2 + \lambda \operatorname{psi}(W)$$

- loss='square-missing' same as loss='square', but handles missing data represented by NaN (not a number) in the matrix  $Y$

- if loss='logistic' and regul is a regularization function for vectors, the entries of  $Y$  are either -1 or +1,  $W = [w^1, \dots, w^n]$  is a matrix of size  $p \times n$  For all column  $y$  of  $Y$ , it computes a column  $w$  of  $W$  such that

$$w = \operatorname{argmin} (1/m) \sum_{j=1}^m \log(1 + e^{-(y_j - x_j^T w)}) + \lambda \operatorname{psi}(w),$$

where  $x^j$  is the  $j$ -th row of  $X$ .

- if loss='logistic' and regul is a regularization function for matrices the entries of  $Y$  are either -1 or +1,  $W$  is a matrix of size  $p \times n$

$$W = \operatorname{argmin} \sum_{i=1}^n (1/m) \sum_{j=1}^m \log(1 + e^{-(y^i - x^j^T w^i)}) + \lambda \operatorname{psi}(W)$$

- if loss='multi-logistic' and regul is a regularization function for vectors, the entries of  $Y$  are in  $\{0, 1, \dots, N\}$  where  $N$  is the total number of classes  $W = [W^1, \dots, W^n]$  is a matrix of size  $p \times Nn$ , each submatrix  $W^i$  is of size  $p \times N$  for all submatrix  $W^i$  of  $W$ , and column  $y$  of  $Y$ , it computes

$$WW = \operatorname{argmin} (1/m) \sum_{j=1}^m \log(\sum_{j=1}^r e^{(x^j)'(ww^j - ww^{y_j})}) + \lambda \sum_{j=1}^N \psi(ww^j),$$

where  $ww^j$  is the  $j$ -th column of  $WW$ .

- if `loss='multi-logistic'` and `regul` is a regularization function for matrices, the entries of  $Y$  are in  $\{0, 1, \dots, N\}$  where  $N$  is the total number of classes  $W$  is a matrix of size  $p \times N$ , it computes

$$W = \operatorname{argmin} (1/m) \sum_{j=1}^m \log(\sum_{j=1}^r e^{(x^j)'(w^j - w^{y_j})}) + \lambda \psi(W)$$

where  $ww^j$  is the  $j$ -th column of  $WW$ .

- **loss='cur' useful to perform sparse CUR matrix decompositions**,  $W = \operatorname{argmin} 0.5 \|Y - X * W * X\|_F^2 + \lambda \psi(W)$

The function `psi` are those used by `proximalFlat` (see documentation)

This function can also handle intercepts (last row of  $W$  is not regularized), and/or non-negativity constraints on  $W$ , and sparse matrices for  $X$

**Args:**  $Y$ : double dense  $m \times n$  matrix  $X$ : double dense or sparse  $m \times p$  matrix  $W0$ : double dense  $p \times n$  matrix or  $p \times N_n$  matrix (for multi-logistic loss)

initial guess

**return\_optim\_info:** if true the function will return a tuple of matrices.

**Kwargs:** `loss`: (choice of loss, see above) `regul`: (choice of regularization, see function `proximalFlat`) `lambda1`: (regularization parameter) `lambda2`: (optional, regularization parameter, 0 by default) `lambda3`: (optional, regularization parameter, 0 by default) `verbose`: (optional, verbosity level, false by default) `pos`: (optional, adds positivity constraints on the

coefficients, false by default)

`transpose`: (optional, transpose the matrix in the regularization function) `size_group`: (optional, for regularization functions assuming a group

structure)

**groups:** (`int32`, optional, for regularization functions assuming a group structure, see `proximalFlat`)

**numThreads:** (optional, number of threads for exploiting multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

`max_it`: (optional, maximum number of iterations, 100 by default) `it0`: (optional, frequency for computing duality gap, every 10 iterations by default) `tol`: (optional, tolerance for stopping criterion, which is a relative duality gap

if it is available, or a relative change of parameters).

`gamma`: (optional, multiplier for increasing the parameter  $L$  in `fista`, 1.5 by default) `L0`: (optional, initial parameter  $L$  in `fista`, 0.1 by default, should be small enough) `fixed_step`: (deactivate the line search for  $L$  in `fista` and use  $L0$  instead) `linesearch_mode`: (line-search scheme when `ista=true`: 0: default, monotonic backtracking scheme 1: monotonic backtracking scheme, with restart at each iteration 2: Barzilai-Borwein step sizes (similar to `SparSA` by Wright et al.) 3: non-monotonic backtracking) `compute_gram`: (optional, pre-compute  $X^T X$ , false by default). `intercept`: (optional, do not regularize last row of  $W$ , false by default). `ista`: (optional, use `ista` instead of `fista`, false by default). `subgrad`: (optional, if not `ista`, use subgradient descent instead of `fista`, false by default). `a`: `b`: (optional, if `subgrad`, the gradient step is  $a/(t+b)$ )

also similar options as proximalFlat

the function also implements the ADMM algorithm via an option `admm=true`. It is not documented and you need to look at the source code to use it.

delta: undocumented; modify at your own risks! c: undocumented; modify at your own risks!  
 max\_iter\_backtracking: undocumented; modify at your own risks! lin\_admm: undocumented; modify at your own risks!  
 admm: undocumented; modify at your own risks! resetflow: undocumented; modify at your own risks!  
 clever: undocumented; modify at your own risks! log: undocumented; modify at your own risks!  
 logName: undocumented; modify at your own risks! is\_inner\_weights: undocumented; modify at your own risks!  
 inner\_weights: undocumented; modify at your own risks! sqrt\_step: undocumented; modify at your own risks!

**Returns:** W: double dense  $p \times n$  matrix or  $p \times N_n$  matrix (for multi-logistic loss) optim: optional, double dense  $4 \times n$  matrix.

first row: values of the objective functions. third row: values of the relative duality gap (if available) fourth row: number of iterations

**optim\_info: vector of size 4, containing information of the optimization.** W =  
`spams.fistaFlat(Y,X,W0,return_optim_info = False,...)` (W,optim\_info) =  
`spams.fistaFlat(Y,X,W0,return_optim_info = True,...)`

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:**

**Valid values for the regularization parameter (regul) are:** "l0", "l1", "l2", "l1f", "l2-not-squared", "elastic-net", "fused-lasso", "group-lasso-l2", "group-lasso-l1f", "sparse-group-lasso-l2", "sparse-group-lasso-l1f", "l1l2", "l1l1f", "l1l2+l1", "l1l1f+l1", "tree-l0", "tree-l2", "tree-l1f", "graph", "graph-ridge", "graph-l2", "multi-task-tree", "multi-task-graph", "l1l1f-row-column", "trace-norm", "trace-norm-vec", "rank", "rank-vec", "none"



## FISTATREE

```
spams.fistaTree(Y, X, W0, tree, return_optim_info=False, numThreads=-1, max_it=1000, L0=1.0,
fixed_step=False, gamma=1.5, lambda1=1.0, delta=1.0, lambda2=0.0, lambda3=0.0,
a=1.0, b=0.0, c=1.0, tol=1e-06, it0=100, max_iter_backtracking=1000, compute_gram=False,
lin_admm=False, admm=False, intercept=False, resetflow=False, regul="", loss="", verbose=False,
pos=False, clever=False, log=False, ista=False, subgrad=False, logName="", is_inner_weights=False,
inner_weights=None, size_group=1, sqrt_step=True, transpose=False, linesearch_mode=0)
```

fistaTree solves sparse regularized problems.

$X$  is a design matrix of size  $m \times p$   $X=[x^1, \dots, x^n]^T$ , where the  $x_i$ 's are the rows of  $X$   
 $Y=[y^1, \dots, y^n]$  is a matrix of size  $m \times n$  It implements the algorithms FISTA, ISTA and subgradient descent for solving

$$\min_W \text{loss}(W) + \lambda_1 \psi(W)$$

The function  $\psi$  are those used by proximalTree (see documentation) for the loss functions, see the documentation of fistaFlat

This function can also handle intercepts (last row of  $W$  is not regularized), and/or non-negativity constraints on  $W$  and sparse matrices  $X$

**Args:**  $Y$ : double dense  $m \times n$  matrix  $X$ : double dense or sparse  $m \times p$  matrix  $W0$ : double dense  $p \times n$  matrix or  $p \times N_n$  matrix (for multi-logistic loss)

initial guess

tree: named list (see documentation of proximalTree) return\_optim\_info:

if true the function will return a tuple of matrices.

**Kwargs:** loss: (choice of loss, see above) regul: (choice of regularization, see function proximalFlat) lambda1: (regularization parameter) lambda2: (optional, regularization parameter, 0 by default) lambda3: (optional, regularization parameter, 0 by default) verbose: (optional, verbosity level, false by default) pos: (optional, adds positivity constraints on the

coefficients, false by default)

transpose: (optional, transpose the matrix in the regularization function) size\_group: (optional, for regularization functions assuming a group

structure)

**numThreads:** (optional, number of threads for exploiting multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

max\_it: (optional, maximum number of iterations, 100 by default) it0: (optional, frequency for computing duality gap, every 10 iterations by default) tol: (optional, tolerance for stopping criterion, which is a relative duality gap

if it is available, or a relative change of parameters).

gamma: (optional, multiplier for increasing the parameter L in fista, 1.5 by default) L0: (optional, initial parameter L in fista, 0.1 by default, should be small enough) fixed\_step: (deactivate the line search for L in fista and use L0 instead) compute\_gram: (optional, pre-compute  $X^T X$ , false by default). intercept: (optional, do not regularize last row of W, false by default). ista: (optional, use ista instead of fista, false by default). subgrad: (optional, if not ista, use subgradient descent instead of fista, false by default). a: b: (optional, if subgrad, the gradient step is  $a/(t+b)$ )

also similar options as proximalTree

the function also implements the ADMM algorithm via an option `admm=true`. It is not documented and you need to look at the source code to use it.

delta: undocumented; modify at your own risks! c: undocumented; modify at your own risks!  
 max\_iter\_backtracking: undocumented; modify at your own risks! lin\_admm: undocumented; modify at your own risks!  
 admm: undocumented; modify at your own risks! resetflow: undocumented; modify at your own risks!  
 clever: undocumented; modify at your own risks! log: undocumented; modify at your own risks!  
 logName: undocumented; modify at your own risks! is\_inner\_weights: undocumented; modify at your own risks!  
 inner\_weights: undocumented; modify at your own risks! sqrt\_step: undocumented; modify at your own risks!

**Returns:** W: double dense  $p \times n$  matrix or  $p \times N_n$  matrix (for multi-logistic loss) optim: optional, double dense  $4 \times n$  matrix.

first row: values of the objective functions. third row: values of the relative duality gap (if available) fourth row: number of iterations

**optim\_info: vector of size 4, containing information of the optimization.** W =  
`spams.fistaTree(Y,X,W0,tree,return_optim_info = False,...)` (W,optim\_info) =  
`spams.fistaTree(Y,X,W0,tree,return_optim_info = True,...)`

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:**

**Valid values for the regularization parameter (regul) are:** "l0", "l1", "l2", "l1f", "l2-not-squared", "elastic-net", "fused-lasso", "group-lasso-l2", "group-lasso-l1f", "sparse-group-lasso-l2", "sparse-group-lasso-l1f", "l1l2", "l1l1f", "l1l2+l1", "l1l1f+l1", "tree-l0", "tree-l2", "tree-l1f", "graph", "graph-ridge", "graph-l2", "multi-task-tree", "multi-task-graph", "l1l1f-row-column", "trace-norm", "trace-norm-vec", "rank", "rank-vec", "none"

## FISTAGRAPH

```
spams.fistaGraph(Y, X, W0, graph, return_optim_info=False, numThreads=-1, max_it=1000,
                 L0=1.0, fixed_step=False, gamma=1.5, lambda1=1.0, delta=1.0,
                 lambda2=0.0, lambda3=0.0, a=1.0, b=0.0, c=1.0, tol=1e-06, it0=100,
                 max_iter_backtracking=1000, compute_gram=False, lin_admm=False,
                 admm=False, intercept=False, resetflow=False, regul="", loss="", verbose=False,
                 pos=False, clever=False, log=False, ista=False, subgrad=False, logName="",
                 is_inner_weights=False, inner_weights=None, size_group=1, sqrt_step=True,
                 transpose=False, linesearch_mode=0)
```

fistaGraph solves sparse regularized problems.

X is a design matrix of size  $m \times p$   $X=[x^1, \dots, x^n]$ , where the  $x_i$ 's are the rows of X  
 $Y=[y^1, \dots, y^n]$  is a matrix of size  $m \times n$  It implements the algorithms FISTA, ISTA and subgradient descent.

It implements the algorithms FISTA, ISTA and subgradient descent for solving

$$\min_W \text{loss}(W) + \lambda_1 \psi(W)$$

The function  $\psi$  are those used by proximalGraph (see documentation) for the loss functions, see the documentation of fistaFlat

This function can also handle intercepts (last row of W is not regularized), and/or non-negativity constraints on W.

**Args:** Y: double dense  $m \times n$  matrix X: double dense or sparse  $m \times p$  matrix W0: double dense  $p \times n$  matrix or  $p \times n$  matrix (for multi-logistic loss)

initial guess

graph: struct (see documentation of proximalGraph) return\_optim\_info:

if true the function will return a tuple of matrices.

**Kwargs:** loss: (choice of loss, see above) regul: (choice of regularization, see function proximalFlat) lambda1: (regularization parameter) lambda2: (optional, regularization parameter, 0 by default) lambda3: (optional, regularization parameter, 0 by default) verbose: (optional, verbosity level, false by default) pos: (optional, adds positivity constraints on the

coefficients, false by default)

**numThreads:** (optional, number of threads for exploiting multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

max\_it: (optional, maximum number of iterations, 100 by default) it0: (optional, frequency for computing duality gap, every 10 iterations by default) tol: (optional, tolerance for stopping criterion, which is a relative duality gap

if it is available, or a relative change of parameters).

gamma: (optional, multiplier for increasing the parameter L in fista, 1.5 by default) L0: (optional, initial parameter L in fista, 0.1 by default, should be small enough) fixed\_step: (deactivate the line search for L in fista and use L0 instead) compute\_gram: (optional, pre-compute  $X^T X$ , false by default). intercept: (optional, do not regularize last row of W, false by default). ista: (optional, use ista instead of fista, false by default). subgrad: (optional, if not ista, use subgradient descent instead of fista, false by default). a: b: (optional, if subgrad, the gradient step is  $a/(t+b)$ )

also similar options as proximalTree

the function also implements the ADMM algorithm via an option `admm=true`. It is not documented and you need to look at the source code to use it.

delta: undocumented; modify at your own risks! c: undocumented; modify at your own risks! max\_iter\_backtracking: undocumented; modify at your own risks! lin\_admm: undocumented; modify at your own risks! admm: undocumented; modify at your own risks! resetflow: undocumented; modify at your own risks! clever: undocumented; modify at your own risks! log: undocumented; modify at your own risks! logName: undocumented; modify at your own risks! is\_inner\_weights: undocumented; modify at your own risks! inner\_weights: undocumented; modify at your own risks! sqrt\_step: undocumented; modify at your own risks! size\_group: undocumented; modify at your own risks! transpose: undocumented; modify at your own risks!

**Returns:** W: double dense  $p \times n$  matrix or  $p \times N_n$  matrix (for multi-logistic loss) optim: optional, double dense  $4 \times n$  matrix.

first row: values of the objective functions. third row: values of the relative duality gap (if available) fourth row: number of iterations

**optim\_info: vector of size 4, containing information of the optimization.** W =  
`spams.fistaGraph(Y,X,W0,graph,return_optim_info = False,...)` (W,optim\_info) =  
`spams.fistaGraph(Y,X,W0,graph,return_optim_info = True,...)`

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:**

**Valid values for the regularization parameter (regul) are:** "l0", "l1", "l2", "l1f", "l2-not-squared", "elastic-net", "fused-lasso", "group-lasso-l2", "group-lasso-l1f", "sparse-group-lasso-l2", "sparse-group-lasso-l1f", "l1l2", "l1l1f", "l1l2+l1", "l1l1f+l1", "tree-l0", "tree-l2", "tree-l1f", "graph", "graph-ridge", "graph-l2", "multi-task-tree", "multi-task-graph", "l1l1f-row-column", "trace-norm", "trace-norm-vec", "rank", "rank-vec", "none"

## PROXIMALFLAT

spams.**proximalFlat** (*U*, *return\_val\_loss=False*, *numThreads=-1*, *lambda1=1.0*, *lambda2=0.0*,  
*lambda3=0.0*, *intercept=False*, *resetflow=False*, *regul=""*, *verbose=False*,  
*pos=False*, *clever=True*, *size\_group=1*, *groups=None*, *transpose=False*)

**proximalFlat computes proximal operators.** Depending on the value of *regul*, it computes

Given an input matrix  $U=[u^1, \dots, u^n]$ , it computes a matrix  $V=[v^1, \dots, v^n]$  such that if one chooses a regularization functions on vectors, it computes for each column  $u$  of  $U$ , a column  $v$  of  $V$  solving if *regul*='l0'

$$\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\|v\|_0$$

**if regul='l1'**  $\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\|v\|_1$

**if regul='l2'**  $\operatorname{argmin} 0.5\|u-v\|_2^2 + 0.5\lambda\|v\|_2^2$

**if regul='elastic-net'**  $\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\|v\|_1 + \lambda_2\|v\|_2^2$

**if regul='fused-lasso'**

$$\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\mathbf{FL}(v) + \dots \dots \lambda_2\|v\|_1 + \lambda_3\|v\|_2^2$$

**if regul='linf'**  $\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\|v\|_{\infty}$

**if regul='l1-constraint'**  $\operatorname{argmin} 0.5\|u-v\|_2^2$  s.t.  $\|v\|_1 \leq \lambda$

**if regul='l2-not-squared'**  $\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\|v\|_2$

**if regul='group-lasso-l2'**  $\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\sum_g \|v_{g\cdot}\|_2$  where the groups are either defined by *groups* or by *size\_group*,

**if regul='group-lasso-linf'**  $\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\sum_g \|v_{g\cdot}\|_{\infty}$

**if regul='sparse-group-lasso-l2'**  $\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\sum_g \|v_{g\cdot}\|_2 + \lambda_2\|v\|_1$  where the groups are either defined by *groups* or by *size\_group*,

**if regul='sparse-group-lasso-linf'**  $\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\sum_g \|v_{g\cdot}\|_{\infty} + \lambda_2\|v\|_1$

**if regul='trace-norm-vec'**

$$\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda\|\operatorname{mat}(v)\|_*$$

where  $\operatorname{mat}(v)$  has *size\_group* rows

if one chooses a regularization function on matrices if *regul*='l1l2',  $V=$

$$\operatorname{argmin} 0.5\|U-V\|_F^2 + \lambda\|V\|_{\{1/2\}}$$

**if regul='l1linf'**,  $V= \operatorname{argmin} 0.5\|U-V\|_F^2 + \lambda\|V\|_{\{1/\infty\}}$

**if regul='l1l2+l1', V=**  $\operatorname{argmin} 0.5\|U-V\|_F^2 + \lambda_1\|V\|_{1/2} + \lambda_2\|V\|_{1/1}$   
**if regul='l1linf+l1', V=**  $\operatorname{argmin} 0.5\|U-V\|_F^2 + \lambda_1\|V\|_{1/\infty} + \lambda_2\|V\|_{1/1}$   
**if regul='l1linf+row-column', V=**  $\operatorname{argmin} 0.5\|U-V\|_F^2 + \lambda_1\|V\|_{1/\infty} + \lambda_2\|V\|_{1/\infty}$   
**if regul='trace-norm', V=**  $\operatorname{argmin} 0.5\|U-V\|_F^2 + \lambda_1\|V\|_*$   
**if regul='rank', V=**  $\operatorname{argmin} 0.5\|U-V\|_F^2 + \lambda_1 \operatorname{rank}(V)$   
**if regul='none', V=**  $\operatorname{argmin} 0.5\|U-V\|_F^2$

for all these regularizations, it is possible to enforce non-negativity constraints with the option `pos`, and to prevent the last row of `U` to be regularized, with the option `intercept`

**Args:**

**U:** double `m x n` matrix (**input signals**) `m` is the signal size

**return\_val\_loss:** if true the function will return a tuple of matrices.

**Kwargs:** `lambda1`: (regularization parameter) `regul`: (choice of regularization, see above) `lambda2`: (optional, regularization parameter) `lambda3`: (optional, regularization parameter) `verbose`: (optional, verbosity level, false by default) `intercept`: (optional, last row of `U` is not regularized, false by default)

`transpose`: (optional, transpose the matrix in the regularization function) `size_group`: (optional, for regularization functions assuming a group

structure). It is a scalar. When `groups` is not specified, it assumes that the groups are the sets of consecutive elements of size `size_group`

**groups:** (`int32`, optional, for regularization functions assuming a group structure. It is an `int32` vector of size `m` containing the group indices of the variables (first group is 1).

**pos:** (optional, adds positivity constraints on the coefficients, false by default)

**numThreads:** (optional, number of threads for exploiting multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

`resetflow`: undocumented; modify at your own risks! `clever`: undocumented; modify at your own risks!

**Returns:** `V`: double `m x n` matrix (output coefficients) `val_regularizer`: double `1 x n` vector (value of the regularization term at the optimum).

**val\_loss:** vector of size `U.shape[1]` `alpha = spams.proximalFlat(U,return_val_loss = False,...)` (`alpha, val_loss = spams.proximalFlat(U,return_val_loss = True,...)`)

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:**

**Valid values for the regularization parameter (regul) are:** "l0", "l1", "l2", "linf", "l2-not-squared", "elastic-net", "fused-lasso", "group-lasso-l2", "group-lasso-linf", "sparse-group-lasso-l2", "sparse-group-lasso-linf", "l1l2", "l1linf", "l1l2+l1", "l1linf+l1", "tree-l0", "tree-l2", "tree-linf", "graph", "graph-ridge", "graph-l2", "multi-task-tree", "multi-task-graph", "l1linf-row-column", "trace-norm", "trace-norm-vec", "rank", "rank-vec", "none"

## PROXIMALTREE

spams.**proximalTree** (*U*, *tree*, *return\_val\_loss=False*, *numThreads=-1*, *lambda1=1.0*, *lambda2=0.0*, *lambda3=0.0*, *intercept=False*, *resetflow=False*, *regul=""*, *verbose=False*, *pos=False*, *clever=True*, *size\_group=1*, *transpose=False*)

**proximalTree** computes a proximal operator. Depending on the value of *regul*, it computes

Given an input matrix  $U=[u^1, \dots, u^n]$ , and a tree-structured set of groups  $T$ , it returns a matrix  $V=[v^1, \dots, v^n]$ :

when the regularization function is for vectors, for every column  $u$  of  $U$ , it compute a column  $v$  of  $V$  solving if *regul*='tree-l0'

$$\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda \sum_{g \in T} \delta^g(v)$$

if *regul*='tree-l2'

$$\text{for all } i, v^i = \operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda \sum_{g \in T} \eta_g \|v_g\|_2$$

if *regul*='tree-linf'

$$\text{for all } i, v^i = \operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda \sum_{g \in T} \eta_g \|v_g\|_{\infty}$$

when the regularization function is for matrices: if *regul*='multi-task-tree'

$$V = \operatorname{argmin} 0.5\|U-V\|_F^2 + \lambda \sum_{i=1}^n \sum_{g \in T} \eta_g \|v^i\|_{\infty} + \dots \\ \lambda \sum_{g \in T} \eta_g \max_{j \in g} \|V_j\|_{\infty}$$

it can also be used with any non-tree-structured regularization addressed by `proximalFlat`

for all these regularizations, it is possible to enforce non-negativity constraints with the option *pos*, and to prevent the last row of  $U$  to be regularized, with the option *intercept*

### Args:

**U:** double  $m \times n$  matrix (input signals)  $m$  is the signal size

**tree:** named list with four fields, *eta\_g*, *groups*, *own\_variables* and *N\_own\_variables*.

The tree structure requires a particular organization of groups and variables \* Let us denote by  $N = |T|$ , the number of groups. the groups should be ordered  $T = \{g_1, g_2, \dots, g_N\}$  such that if  $g_i$  is included in  $g_j$ , then  $j < i$ .  $g_1$  should be the group at the root of the tree and contains every variable. \* Every group is a set of contiguous indices for instance  $g_i = \{3, 4, 5\}$  or  $g_i = \{4, 5, 6, 7\}$  or  $g_i = \{4\}$ , but not  $\{3, 5\}$ ; \* We define  $\operatorname{root}(g_i)$  as the indices of the variables that are in  $g_i$ , but not in its descendants. For instance for  $T = \{g_1 = \{1, 2, 3, 4\}, g_2 = \{2, 3\}, g_3 = \{4\}\}$ , then,  $\operatorname{root}(g_1) = \{1\}$ ,  $\operatorname{root}(g_2) = \{2, 3\}$ ,  $\operatorname{root}(g_3) = \{4\}$ . We assume that for all  $i$ ,  $\operatorname{root}(g_i)$  is a set of contiguous variables \* We assume that the smallest of  $\operatorname{root}(g_i)$  is also the smallest index of  $g_i$ .

For instance,  $T = \{ g_1 = \{1, 2, 3, 4\}, g_2 = \{2, 3\}, g_3 = \{4\} \}$ , is a valid set of groups. but we can not have  $T = \{ g_1 = \{1, 2, 3, 4\}, g_2 = \{1, 2\}, g_3 = \{3\} \}$ , since  $\text{root}(g_1) = \{4\}$  and 4 is not the smallest element in  $g_1$ .

We do not lose generality with these assumptions since they can be fulfilled for any tree-structured set of groups after a permutation of variables and a correct ordering of the groups. see more examples in `test_ProximalTree.m` of valid tree-structured sets of groups.

The first field sets the weights for every group `tree['eta_g']` double N vector

The next field sets inclusion relations between groups (but not between groups and variables): `tree['groups']` sparse (double or boolean) N x N matrix the (i,j) entry is non-zero if and only if i is different than j and  $g_i$  is included in  $g_j$ . the first column corresponds to the group at the root of the tree.

The next field define the smallest index of each group  $g_i$ , which is also the smallest index of  $\text{root}(g_i)$  `tree['own_variables']` int32 N vector

The next field define for each group  $g_i$ , the size of  $\text{root}(g_i)$  `tree['N_own_variables']` int32 N vector

examples are given in `test_ProximalTree.m`

**return\_val\_loss:** if true the function will return a tuple of matrices.

**Kwargs:** `lambda1`: (regularization parameter) `regul`: (choice of regularization, see above) `lambda2`: (optional, regularization parameter) `lambda3`: (optional, regularization parameter) `verbose`: (optional, verbosity level, false by default) `intercept`: (optional, last row of U is not regularized, false by default)

**pos:** (optional, adds positivity constraints on the coefficients, false by default)

`transpose`: (optional, transpose the matrix in the regularization function) `size_group`: (optional, for regularization functions assuming a group

structure). It is a scalar. When `groups` is not specified, it assumes that the groups are the sets of consecutive elements of size `size_group`

**numThreads:** (optional, number of threads for exploiting multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

`resetflow`: undocumented; modify at your own risks! `clever`: undocumented; modify at your own risks!

**Returns:** V: double m x n matrix (output coefficients) `val_regularizer`: double 1 x n vector (value of the regularization

term at the optimum).

**val\_loss:** vector of size `U.shape[1]` `alpha = spams.proximalTree(U,tree,return_val_loss = False,...)` (`alpha, val_loss = spams.proximalTree(U,tree,return_val_loss = True,...)`)

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:**

**Valid values for the regularization parameter (regul) are:** "l0", "l1", "l2", "l1nf", "l2-not-squared", "elastic-net", "fused-lasso", "group-lasso-l2", "group-lasso-l1nf", "sparse-group-lasso-l2", "sparse-group-lasso-l1nf", "l1l2", "l1l1nf", "l1l2+l1", "l1l1nf+l1", "tree-l0", "tree-l2", "tree-l1nf", "graph", "graph-ridge", "graph-l2", "multi-task-tree", "multi-task-graph", "l1l1nf-row-column", "trace-norm", "trace-norm-vec", "rank", "rank-vec", "none"

## PROXIMALGRAPH

spams.**proximalGraph** (*U*, *graph*, *return\_val\_loss=False*, *numThreads=-1*, *lambda1=1.0*, *lambda2=0.0*,  
*lambda3=0.0*, *intercept=False*, *resetflow=False*, *regul=""*, *verbose=False*,  
*pos=False*, *clever=True*, *eval=None*, *size\_group=1*, *transpose=False*)

**proximalGraph** computes a proximal operator. Depending on the value of *regul*, it computes

Given an input matrix  $U=[u^1, \dots, u^n]$ , and a set of groups  $G$ , it computes a matrix  $V=[v^1, \dots, v^n]$  such that

if *regul*='graph' for every column  $u$  of  $U$ , it computes a column  $v$  of  $V$  solving

$$\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda_1 \sum_{g \in G} \eta_g \|v\|_g \text{inf}$$

if *regul*='graph+ridge' for every column  $u$  of  $U$ , it computes a column  $v$  of  $V$  solving

$$\operatorname{argmin} 0.5\|u-v\|_2^2 + \lambda_1 \sum_{g \in G} \eta_g \|v\|_g \text{inf} + \lambda_2 \|v\|_2^2$$

if *regul*='multi-task-graph'

$$V = \operatorname{argmin} 0.5\|U-V\|_F^2 + \lambda_1 \sum_{i=1}^n \sum_{g \in G} \eta_g \|v^i\|_g \text{inf} + \dots \\ \lambda_2 \sum_{g \in G} \eta_g \max_{j \in g} \|V_j\|_g \text{inf}$$

it can also be used with any regularization addressed by `proximalFlat`

for all these regularizations, it is possible to enforce non-negativity constraints with the option *pos*, and to prevent the last row of  $U$  to be regularized, with the option *intercept*

### Args:

**U:** double  $p \times n$  matrix (input signals)  $m$  is the signal size

**graph:** struct with three fields, *eta\_g*, *groups*, and *groups\_var*

The first field sets the weights for every group *graph.eta\_g* double  $N$  vector

The next field sets inclusion relations between groups (but not between groups and variables): *graph.groups* sparse (double or boolean)  $N \times N$  matrix the  $(i,j)$  entry is non-zero if and only if  $i$  is different than  $j$  and  $g_i$  is included in  $g_j$ .

The next field sets inclusion relations between groups and variables *graph.groups\_var* sparse (double or boolean)  $p \times N$  matrix the  $(i,j)$  entry is non-zero if and only if the variable  $i$  is included in  $g_j$ , but not in any children of  $g_j$ .

examples are given in `test_ProximalGraph.m`

**return\_val\_loss:** if true the function will return a tuple of matrices.

**Kwargs:** lambda1: (regularization parameter) regul: (choice of regularization, see above) lambda2: (optional, regularization parameter) lambda3: (optional, regularization parameter) verbose: (optional, verbosity level, false by default) intercept: (optional, last row of U is not regularized, false by default)

**pos:** (optional, adds positivity constraints on the coefficients, false by default)

**numThreads:** (optional, number of threads for exploiting multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

resetflow: undocumented; modify at your own risks! clever: undocumented; modify at your own risks! size\_group: undocumented; modify at your own risks! transpose: undocumented; modify at your own risks!

**Returns:** V: double  $p \times n$  matrix (output coefficients) val\_regularizer: double  $1 \times n$  vector (value of the regularization

term at the optimum).

**val\_loss:** vector of size `U.shape[1]` alpha = `spams.proximalGraph(U,graph,return_val_loss = False,...)`  
 (alpha,val\_loss) = `spams.proximalGraph(U,graph,return_val_loss = True,...)`

Authors: Julien MAIRAL, 2010 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:**

**Valid values for the regularization parameter (regul) are:** "l0", "l1", "l2", "linf", "l2-not-squared", "elastic-net", "fused-lasso", "group-lasso-l2", "group-lasso-linf", "sparse-group-lasso-l2", "sparse-group-lasso-linf", "l1l2", "l1linf", "l1l2+l1", "l1linf+l1", "tree-l0", "tree-l2", "tree-linf", "graph", "graph-ridge", "graph-l2", "multi-task-tree", "multi-task-graph", "l1linf-row-column", "trace-norm", "trace-norm-vec", "rank", "rank-vec", "none"

## TRAINDL

`spams.trainDL(X, return_model=False, model=None, D=None, numThreads=-1, batchSize=-1, K=-1, lambda1=None, lambda2=1e-09, iter=-1, t0=1e-05, mode=2, posAlpha=False, posD=False, expand=False, modeD=0, whiten=False, clean=True, verbose=True, gamma1=0.0, gamma2=0.0, rho=1.0, iter_updateD=None, stochastic_deprecated=False, modeParam=0, batch=False, log_deprecated=False, logName=")`

trainDL is an efficient implementation of the dictionary learning technique presented in

“Online Learning for Matrix Factorization and Sparse Coding” by Julien Mairal, Francis Bach, Jean Ponce and Guillermo Sapiro arXiv:0908.0050

“Online Dictionary Learning for Sparse Coding” by Julien Mairal, Francis Bach, Jean Ponce and Guillermo Sapiro ICML 2009.

Note that if you use mode=1 or 2, if the training set has a reasonable size and you have enough memory on your computer, you should use trainDL\_Memory instead.

### It addresses the dictionary learning problems

1. if mode=0

$$\min_{\{D \text{ in } C\}} (1/n) \sum_{i=1}^n (1/2) \|x_i - D\alpha_i\|_2^2 \text{ s.t. } \dots$$

$$\|\alpha_i\|_1 \leq \lambda$$

2. if mode=1

$$\min_{\{D \text{ in } C\}} (1/n) \sum_{i=1}^n \|\alpha_i\|_1 \text{ s.t. } \dots$$

$$\|x_i - D\alpha_i\|_2^2 \leq \lambda$$

3. if mode=2

$$\min_{\{D \text{ in } C\}} (1/n) \sum_{i=1}^n (1/2) \|x_i - D\alpha_i\|_2^2 + \dots$$

$$\lambda \|\alpha_i\|_1 + \lambda_2 \|\alpha_i\|_2^2$$

4. if mode=3, the sparse coding is done with OMP

$$\min_{\{D \text{ in } C\}} (1/n) \sum_{i=1}^n (1/2) \|x_i - D\alpha_i\|_2^2 \text{ s.t. } \dots$$

$$\|\alpha_i\|_0 \leq \lambda$$

5. if mode=4, the sparse coding is done with OMP

$$\min_{\{D \text{ in } C\}} (1/n) \sum_{i=1}^n \|\alpha_i\|_0 \text{ s.t. } \dots$$

$$\|x_i - D\alpha_{i,j}\|_2^2 \leq \lambda$$

- if mode=5, the sparse coding is done with OMP

$$\min_{\{D \in C\}} (1/n) \sum_{i=1}^n 0.5 \|x_i - D\alpha_{i,j}\|_2^2 + \lambda \|\alpha_{i,j}\|_0$$

**C is a convex set verifying**

- if modeD=0  $C = \{ D \in \text{Real}^{m \times p} \text{ s.t. } \forall j, \|d_{j,\cdot}\|_2^2 \leq 1 \}$
- if modeD=1  $C = \{ D \in \text{Real}^{m \times p} \text{ s.t. } \forall j, \|d_{j,\cdot}\|_2^2 + \dots + \gamma_1 \|d_{j,1}\|_1 \leq 1 \}$
- if modeD=2  $C = \{ D \in \text{Real}^{m \times p} \text{ s.t. } \forall j, \|d_{j,\cdot}\|_2^2 + \dots + \gamma_1 \|d_{j,1}\|_1 + \gamma_2 \text{FL}(d_j) \leq 1 \}$
- if modeD=3  $C = \{ D \in \text{Real}^{m \times p} \text{ s.t. } \forall j, (1-\gamma_1)\|d_{j,\cdot}\|_2^2 + \dots + \gamma_1 \|d_{j,1}\|_1 \leq 1 \}$

Potentially, n can be very large with this algorithm.

**Args:**

**X: double m x n matrix (input signals)** m is the signal size n is the number of signals to decompose

**return\_model:** if true the function will return the model as a named list ('A' = A, 'B' = B, 'iter' = n)

model: None or model (as A,B,iter) to use as initialisation

**Kwargs:**

**D: (optional) double m x p matrix (dictionary)** p is the number of elements in the dictionary When D is not provided, the dictionary is initialized with random elements from the training set.

**K:** (size of the dictionary, optional is D is provided) **lambda1:** (parameter) **lambda2:** (optional, by default 0) **iter:** (number of iterations). If a negative number is

provided it will perform the computation during the corresponding number of seconds. For instance iter=-5 learns the dictionary during 5 seconds.

**mode:** (optional, see above, by default 2) **posAlpha:** (optional, adds positivity constraints on the coefficients, false by default, not compatible with mode =3,4)

**modeD:** (optional, see above, by default 0) **posD:** (optional, adds positivity constraints on the dictionary, false by default, not compatible with modeD=2)

**gamma1:** (optional parameter for modeD >= 1) **gamma2:** (optional parameter for modeD = 2) **batchsize:** (optional, size of the minibatch, by default

512.

**iter\_updatedD:** (optional, number of BCD iterations for the dictionary update step, by default 1)

**modeParam: (optimization mode).** 1) if modeParam=0, the optimization uses the parameter free strategy of the ICML paper 2) if modeParam=1, the optimization uses the parameters rho as in arXiv:0908.0050 3) if modeParam=2, the optimization uses exponential decay weights with updates of the form  $A_{t+1} \leftarrow \rho A_t + \alpha_t \alpha_t^T$

**rho:** (optional) tuning parameter (see paper arXiv:0908.0050) **t0:** (optional) tuning parameter (see paper arXiv:0908.0050) **clean:** (optional, true by default. prunes

automatically the dictionary from unused elements).

verbose: (optional, true by default, increase verbosity) numThreads: (optional, number of threads for exploiting

multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

expand: undocumented; modify at your own risks! whiten: undocumented; modify at your own risks! stochastic\_deprecated: undocumented; modify at your own risks! batch: undocumented; modify at your own risks! log\_deprecated: undocumented; modify at your own risks! logName: undocumented; modify at your own risks!

**Returns:** D: double m x p matrix (dictionary) model: the model as A B iter

D = spams.trainDL(X,return\_model = False,...) (D,model) = spams.trainDL(X,return\_model = True,...)

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting



## STRUCTTRAINDL

```
spams.structTrainDL(X, return_model=False, model=None, D=None, graph=None, tree=None,
                    numThreads=-1, tol=1e-06, fixed_step=True, ista=False, batchsize=-1,
                    K=-1, lambda1=None, lambda2=1e-09, lambda3=0.0, iter=-1, t0=1e-05,
                    regul='none', posAlpha=False, posD=False, expand=False, modeD=0,
                    whiten=False, clean=True, verbose=True, gamma1=0.0, gamma2=0.0, rho=1.0,
                    iter_updateD=None, stochastic_deprecated=False, modeParam=0, batch=False,
                    log_deprecated=False, logName="")
```

structTrainDL is an efficient implementation of the dictionary learning technique presented in

“Online Learning for Matrix Factorization and Sparse Coding” by Julien Mairal, Francis Bach, Jean Ponce and Guillermo Sapiro arXiv:0908.0050

“Online Dictionary Learning for Sparse Coding” by Julien Mairal, Francis Bach, Jean Ponce and Guillermo Sapiro ICML 2009.

**It addresses the dictionary learning problems**  $\min_{\{D \in C\}} (1/n) \sum_{i=1}^n 0.5\|x_i - D\alpha_i\|_2^2 + \lambda \psi(\alpha)$  where the regularization function  $\psi$  depends on `regul` (see `proximalFlat` for the description of  $\psi$ ,

and `regul` below for allowed values of `regul`)

**C is a convex set verifying**

1. if `modeD=0`  $C = \{ D \in \text{Real}^{m \times p} \text{ s.t. } \forall j, \|d_j\|_2^2 \leq 1 \}$
2. if `modeD=1`  $C = \{ D \in \text{Real}^{m \times p} \text{ s.t. } \forall j, \|d_j\|_2^2 + \dots + \gamma_1 \|d_j\|_1 \leq 1 \}$
3. if `modeD=2`  $C = \{ D \in \text{Real}^{m \times p} \text{ s.t. } \forall j, \|d_j\|_2^2 + \dots + \gamma_1 \|d_j\|_1 + \gamma_2 \text{FL}(d_j) \leq 1 \}$
4. if `modeD=3`  $C = \{ D \in \text{Real}^{m \times p} \text{ s.t. } \forall j, (1-\gamma_1)\|d_j\|_2^2 + \dots + \gamma_1 \|d_j\|_1 \leq 1 \}$

Potentially,  $n$  can be very large with this algorithm.

**Args:**

**X:** double  $m \times n$  matrix (input signals)  $m$  is the signal size  $n$  is the number of signals to decompose

**return\_model:** if true the function will return the model as a named list ('A' = A, 'B' = B, 'iter' = n)

model: None or model (as A,B,iter) to use as initialisation

**Kwargs:**

**D:** (optional) double  $m \times p$  matrix (dictionary)  $p$  is the number of elements in the dictionary When  $D$  is not provided, the dictionary is initialized with random elements from the training set.

**K:** (size of the dictionary, optional is  $D$  is provided) **lambda1:** (parameter) **lambda2:** (optional, by default 0) **lambda3:** (optional, regularization parameter, 0 by default) **iter:** (number of iterations). If a negative number is

provided it will perform the computation during the corresponding number of seconds. For instance `iter=-5` learns the dictionary during 5 seconds.

**regul: choice of regularization** [one of] 'l0' 'l1' 'l2' 'linf' 'none' 'elastic-net' 'fused-lasso' 'graph' 'graph-ridge' 'graph-l2' 'tree-l0' 'tree-l2' 'tree-linf'

**tree: struct** (see documentation of `proximalTree`); needed for regul of graph kind.

**graph: struct** (see documentation of `proximalGraph`); needed for regul of tree kind.

**posAlpha:** (optional, adds positivity constraints on the coefficients, false by default.

**modeD:** (optional, see above, by default 0) **posD:** (optional, adds positivity constraints on the dictionary, false by default, not compatible with `modeD=2`)

**gamma1:** (optional parameter for `modeD >= 1`) **gamma2:** (optional parameter for `modeD = 2`) **batchsize:** (optional, size of the minibatch, by default

512.

**iter\_updatedD:** (optional, number of BCD iterations for the dictionary update step, by default 1)

**modeParam: (optimization mode).** 1) if `modeParam=0`, the optimization uses the parameter free strategy of the ICML paper 2) if `modeParam=1`, the optimization uses the parameters  $\rho$  as in arXiv:0908.0050 3) if `modeParam=2`, the optimization uses exponential decay weights with updates of the form  $A_{\{t\}} <- \rho A_{\{t-1\}} + \alpha_t \alpha_t^T$

**ista:** (optional, use ista instead of fista, false by default). **tol:** (optional, tolerance for stopping criterion, which is a relative duality gap **fixed\_step:** (deactivate the line search for  $L$  in fista and use  $K$  instead) **rho:** (optional) tuning parameter (see paper arXiv:0908.0050) **t0:** (optional) tuning parameter (see paper arXiv:0908.0050) **clean:** (optional, true by default. prunes

automatically the dictionary from unused elements).

**verbose:** (optional, true by default, increase verbosity) **numThreads:** (optional, number of threads for exploiting

multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

**expand:** undocumented; modify at your own risks! **whiten:** undocumented; modify at your own risks! **stochastic\_deprecated:** undocumented; modify at your own risks! **batch:** undocumented; modify at your own risks! **log\_deprecated:** undocumented; modify at your own risks! **logName:** undocumented; modify at your own risks!

**Returns:**  $D$ : double  $m \times p$  matrix (dictionary) **model:** the model as  $A B$  **iter**

```
D = spams.structTrainDL(X,return_model = False,...) (D,model) =
spams.structTrainDL(X,return_model = True,...)
```

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting



## TRAINDL\_MEMORY

```
spams.trainDL_Memory (X, D=None, numThreads=-1, batchSize=-1, K=-1, lambda1=None, iter=-1,
                      t0=1e-05, mode=2, posD=False, expand=False, modeD=0, whiten=False,
                      clean=True, gamma1=0.0, gamma2=0.0, rho=1.0, iter_updateD=1, stochastic_deprecated=False,
                      modeParam=0, batch=False, log_deprecated=False, logName="")
```

trainDL\_Memory is an efficient but memory consuming variant of the dictionary learning technique presented in

“Online Learning for Matrix Factorization and Sparse Coding” by Julien Mairal, Francis Bach, Jean Ponce and Guillermo Sapiro arXiv:0908.0050

“Online Dictionary Learning for Sparse Coding” by Julien Mairal, Francis Bach, Jean Ponce and Guillermo Sapiro ICML 2009.

**Contrary to the approaches above, the algorithm here** does require to store all the coefficients from all the training signals. For this reason this variant can not be used with large training sets, but is more efficient than the regular online approach for training sets of reasonable size.

**It addresses the dictionary learning problems**

1. if mode=1

$\min_{\{D \text{ in } C\}} (1/n) \sum_{i=1}^n \|\alpha_{ill\_1}\|$  s.t. ...

$$\|x_i - D\alpha_{ill\_2}\|^2 \leq \lambda$$

2. if mode=2

$\min_{\{D \text{ in } C\}} (1/n) \sum_{i=1}^n (1/2)\|x_i - D\alpha_{ill\_2}\|^2 + \dots \lambda \|\alpha_{ill\_1}\|$

**C is a convex set verifying**

1. if modeD=0  $C = \{ D \text{ in } \mathbb{R}^{m \times p} \text{ s.t. } \forall j, \|d_{jll\_2}\|^2 \leq 1 \}$

1. if modeD=1  $C = \{ D \text{ in } \mathbb{R}^{m \times p} \text{ s.t. } \forall j, \|d_{jll\_2}\|^2 + \dots \gamma_1 \|d_{jll\_1}\| \leq 1 \}$

1. if modeD=2  $C = \{ D \text{ in } \mathbb{R}^{m \times p} \text{ s.t. } \forall j, \|d_{jll\_2}\|^2 + \dots \gamma_1 \|d_{jll\_1}\| + \gamma_2 \text{FL}(d_j) \leq 1 \}$

Potentially, n can be very large with this algorithm.

**Args:**

**X:** double m x n matrix (input signals) m is the signal size n is the number of signals to decompose

**Kwargs:**

**D: (optional) double m x p matrix (dictionary)** p is the number of elements in the dictionary When D is not provided, the dictionary is initialized with random elements from the training set.

**K:** (size of the dictionary, optional is D is provided) **lambda1:** (parameter) **iter:** (number of iterations). If a negative number is

provided it will perform the computation during the corresponding number of seconds. For instance `iter=-5` learns the dictionary during 5 seconds.

**mode:** (optional, see above, by default 2) **modeD:** (optional, see above, by default 0) **posD:** (optional, adds positivity constraints on the

dictionary, false by default, not compatible with `modeD=2`)

**gamma1:** (optional parameter for `modeD >= 1`) **gamma2:** (optional parameter for `modeD = 2`) **batchsize:** (optional, size of the minibatch, by default

512.

**iter\_updatedD:** (optional, number of BCD iterations for the dictionary update step, by default 1)

**modeParam: (optimization mode).** 1) if `modeParam=0`, the optimization uses the parameter free strategy of the ICML paper 2) if `modeParam=1`, the optimization uses the parameters  $\rho$  as in arXiv:0908.0050 3) if `modeParam=2`, the optimization uses exponential decay weights with updates of the form  $A_{\{t\}} \leftarrow \rho A_{\{t-1\}} + \alpha_t \alpha_t^T$

**rho:** (optional) tuning parameter (see paper arXiv:0908.0050) **t0:** (optional) tuning parameter (see paper arXiv:0908.0050) **clean:** (optional, true by default. prunes

automatically the dictionary from unused elements).

**numThreads: (optional, number of threads for exploiting** multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

**expand:** undocumented; modify at your own risks! **whiten:** undocumented; modify at your own risks! **stochastic\_deprecated:** undocumented; modify at your own risks! **batch:** undocumented; modify at your own risks! **log\_deprecated:** undocumented; modify at your own risks! **logName:** undocumented; modify at your own risks!

**Returns:** D: double m x p matrix (dictionary) model: the model as A B iter

`D = spams.trainDL_Memory(X,...)`

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

**Note:** this function admits a few experimental usages, which have not been extensively tested:

- single precision setting (even though the output  $\alpha$  is double precision)

## NMF

`spams.nmf` ( $X$ , `return_lasso=False`, `model=None`, `numThreads=-1`, `batchsize=-1`, `K=-1`, `iter=-1`, `t0=1e-05`,  
`clean=True`, `rho=1.0`, `modeParam=0`, `batch=False`)

`trainDL` is an efficient implementation of the non-negative matrix factorization technique presented in

“Online Learning for Matrix Factorization and Sparse Coding” by Julien Mairal, Francis Bach, Jean Ponce and Guillermo Sapiro arXiv:0908.0050

“Online Dictionary Learning for Sparse Coding” by Julien Mairal, Francis Bach, Jean Ponce and Guillermo Sapiro ICML 2009.

Potentially,  $n$  can be very large with this algorithm.

### Args:

**X:** double  $m \times n$  matrix (input signals)  $m$  is the signal size  $n$  is the number of signals to decompose

**return\_lasso:** if true the function will return a tuple of matrices.

**Kwargs:** **K:** (number of required factors) **iter:** (number of iterations). If a negative number

is provided it will perform the computation during the corresponding number of seconds. For instance `iter=-5` learns the dictionary during 5 seconds.

**batchsize:** (optional, size of the minibatch, by default

512.

**modeParam:** (optimization mode). 1) if `modeParam=0`, the optimization uses the parameter free strategy of the ICML paper 2) if `modeParam=1`, the optimization uses the parameters `rho` as in arXiv:0908.0050 3) if `modeParam=2`, the optimization uses exponential decay weights with updates of the form  $A_{\{t\}} \leftarrow \rho A_{\{t-1\}} + \alpha_t \alpha_t^T$

**rho:** (optional) tuning parameter (see paper arXiv:0908.0050)

**t0:** (optional) tuning parameter (see paper arXiv:0908.0050)

**clean:** (optional, true by default. prunes automatically the dictionary from unused elements).

**batch:** (optional, false by default, use batch learning instead of online learning)

**numThreads:** (optional, number of threads for exploiting multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

**model:** struct (optional) learned model for “retraining” the data.

**Returns:** **U:** double  $m \times p$  matrix **V:** double  $p \times n$  matrix (optional) **model:** struct (optional) learned model to be used for

“retraining” the data. `U = spams.nmf(X,return_lasso = False,...)` `(U,V) =`  
`spams.nmf(X,return_lasso = True,...)`

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012  
(python interface)

`spams.nnsc` (*X*, *return\_lasso=False*, *model=None*, *lambda1=None*, *numThreads=-1*, *batchsize=-1*, *K=-1*,  
*iter=-1*, *t0=1e-05*, *clean=True*, *rho=1.0*, *modeParam=0*, *batch=False*)

`trainDL` is an efficient implementation of the non-negative sparse coding technique presented in

“Online Learning for Matrix Factorization and Sparse Coding” by Julien Mairal, Francis Bach, Jean Ponce and Guillermo Sapiro arXiv:0908.0050

“Online Dictionary Learning for Sparse Coding” by Julien Mairal, Francis Bach, Jean Ponce and Guillermo Sapiro ICML 2009.

Potentially, *n* can be very large with this algorithm.

**Args:**

**X:** double *m* x *n* matrix (input signals) *m* is the signal size *n* is the number of signals to decompose

**return\_lasso:** if true the function will return a tuple of matrices.

**Kwargs:** *K*: (number of required factors) *lambda1*: (parameter) *iter*: (number of iterations). If a negative number

is provided it will perform the computation during the corresponding number of seconds. For instance *iter=-5* learns the dictionary during 5 seconds.

**batchsize:** (optional, size of the minibatch, by default

512.

**modeParam:** (optimization mode). 1) if *modeParam=0*, the optimization uses the parameter free strategy of the ICML paper 2) if *modeParam=1*, the optimization uses the parameters *rho* as in arXiv:0908.0050 3) if *modeParam=2*, the optimization uses exponential decay weights with updates of the form  $A_{\{t\}} \leftarrow \rho A_{\{t-1\}} + \alpha_t \alpha_t^T$

**rho:** (optional) tuning parameter (see paper arXiv:0908.0050)

**t0:** (optional) tuning parameter (see paper arXiv:0908.0050)

**clean:** (optional, true by default. prunes automatically the dictionary from unused elements).

**batch:** (optional, false by default, use batch learning instead of online learning)

**numThreads:** (optional, number of threads for exploiting multi-core / multi-cpus. By default, it takes the value -1, which automatically selects all the available CPUs/cores).

*model*: struct (optional) learned model for “retraining” the data.

**Returns:** *U*: double *m* x *p* matrix *V*: double *p* x *n* matrix (optional) *model*: struct (optional) learned model to be used for

“retraining” the data. `U = spams.nnsc(X,return_lasso = False,...)` `(U,V) = spams.nnsc(X,return_lasso = True,...)`

Authors: Julien MAIRAL, 2009 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)

## ARCHETYPALANALYSIS

`spams.archetypalAnalysis` (*X*, *p=10*, *Z0=None*, *returnAB=False*, *robust=False*, *epsilon=0.001*,  
*computeXtX=False*, *stepsFISTA=3*, *stepsAS=50*, *randominit=False*,  
*numThreads=-1*)

documentation to appear soon

**Args:**

**X: double m x n matrix (input signals)** *m* is the signal size *n* is the number of signals to decompose

**Returns:** *Z*: double %

Authors: Yuansi Chen and Julien MAIRAL, 2014 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## DECOMPSIMPLEX

`spams.decompSimplex(X, Z, computeXtX=False, numThreads=-1)`

documentation to appear soon

**Args:**

**X: double m x n matrix (input signals)** m is the signal size n is the number of signals to decompose

**Returns:** Z: double %

Authors: Yuansi Chen and Julien MAIRAL, 2014 (spams, matlab interface and documentation) Jean-Paul CHIEZE 2011-2012 (python interface)



## SIMPLEGROUPTREE

spams.**simpleGroupTree** (*degrees*)

    makes a structure representing a tree given the  
    degree of each level.

**Args:** degrees: int vector; degrees(i) is the number of children of each node at level i

**Returns:**

**group\_struct: list, one element for each node** an element is itself a 4 elements list : nodeid (int >= 0), weight (double), array of vars attached to the node (here equal to [nodeid]), array of children (nodeid's)

Authors: Jean-Paul CHIEZE, 2012



## READGROUPSTRUCT

spams . **readGroupStruct** (*file*)

reads a text file describing “simply” the structure of groups of variables needed by proximalGraph, proximalTree, fistaGraph, fistaTree and structTrainDL and builds the corresponding group structure.

weight is a float variables-list : a space separated list of integers, maybe empty, but '[' and ']' must be present. Numbers in the range (0 - Nv-1)

**children-list** [a space separated list of node-id's] If the list is empty, '->' may be omitted.

**The data must obey some rules** []

- A group contains the variables of the corresponding node and of the whole subtree.
- Variables attached to a node are those that are not in the subtree.
- **If the data destination is a Graph, there may be several independant trees,** and a variable may appear in several trees.

**If the destination is a Tree, there must be only one tree, the root node** must have id == 0 and each variable must appear only once.

**Args:** file: the file name

**Returns:**

**groups: list, one element for each node** an element is itself a 4 elements list: nodeid (int >= 0), weight (double), array of vars of the node, array of children (nodeid's)

Authors: Jean-Paul CHIEZE, 2012



## GROUPSTRUCTOFSTRING

`spams.groupStructOfString(s)`

decode a multi-line string describing “simply” the structure of groups of variables needed by `proximalGraph`, `proximalTree`, `fistaGraph`, `fistaTree` and `structTrainDL` and builds the corresponding group structure.

Each line describes a group of variables as a node of a tree. It has up to 4 fields separated by spaces:

node-id node-weight [variables-list] -> children-list

Let's define  $N_g$  = number of groups, and  $N_v$  = number of variables. node-id must be in the range (0 -  $N_g-1$ ), and there must be  $N_g$  nodes weight is a float variables-list : a space separated list of integers, maybe empty,

but '[' and ']' must be present. Numbers in the range (0 -  $N_v-1$ )

**children-list** [a space separated list of node-id's] If the list is empty, '->' may be omitted.

**The data must obey some rules** []

- A group contains the variables of the corresponding node and of the whole subtree.
- Variables attached to a node are those that are not in the subtree.
- If the data destination is a Graph, there may be several independent trees, and a variable may appear in several trees.

If the destination is a Tree, there must be only one tree, the root node must have `id == 0` and each variable must appear only once.

**Args:** `s`: the multi-lines string

**Returns:**

**groups: list, one element for each node** an element is itself a 4 elements list: `nodeid` (int  $\geq 0$ ), `weight` (double), array of vars of the node, array of children (nodeid's)

Authors: Jean-Paul CHIEZE, 2012



## GRAPHOFGROUPSTRUCT

spams.**graphOfGroupStruct** (*gstruct*)

converts a group structure into the graph structure  
used by proximalGraph, fistaGraph or structTrainDL

**Args:**

**gstruct: the structure of groups as a list, one element per node** an element is itself a 4 elements list:  
nodeid ( $\geq 0$ ), weight (double), array of vars associated to the node, array of children (nodeis's)

**Returns:** graph: struct (see documentation of proximalGraph)

Authors: Jean-Paul CHIEZE, 2012



## TREEOFGROUPSTRUCT

`spams.treeOfGroupStruct` (*gstruct*)

converts a group structure into the tree structure  
used by `proximalTree`, `fistaTree` or `structTrainDL`

**Args:**

**gstruct: the structure of groups as a list, one element per node** an element is itself a 4 elements list:  
nodeid ( $\geq 0$ ), weight (double), array of vars associated to the node, array of children (nodeis's)

**Returns:**

**permutations: permutation vector that must be applied to the result of the** programm using the tree.  
Empty if no permutation is needed.

tree: named list (see documentation of `proximalTree`) nbvars: number of variables in the tree  
(permutations,tree,nbvars) = `spams.treeOfGroupStruct(gstruct)`

Authors: Jean-Paul CHIEZE, 2012



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