

ULTIMATE GEMCUTTER

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Example Program

$\{ x = y = i = j = 0 \}$

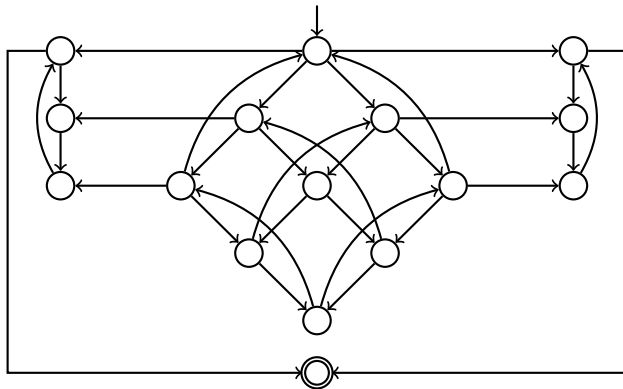
```
while (i < n) {  
    x += A[i];  
    i++;  
}
```

\parallel

```
while (j < n) {  
    y += A[j];  
    j++;  
}
```

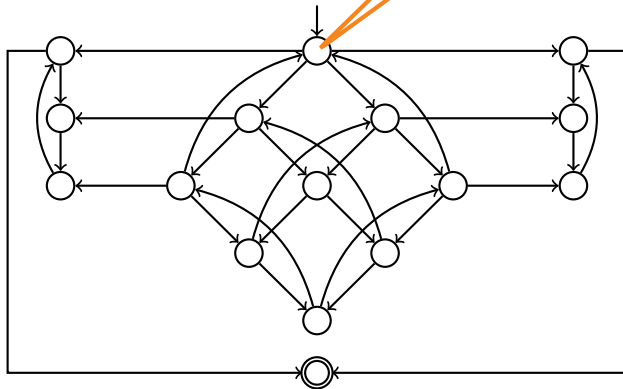
$\{ x = y \}$

Key Idea

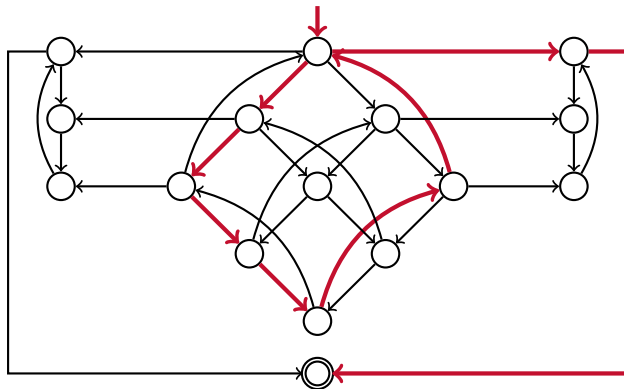


Key Idea

Invariant: $x = \sum_{k=0}^i A[k] \wedge y = \sum_{k=0}^j A[k] \wedge i \leq n \wedge j \leq n$



Key Idea



Counterexample:

$\tau =$ i < n x += A[i] j < n y += A[j] i ++ j ++ i >= n j >= n

Generalization

`i < n`

`x += A[i]`

`j < n`

`y += A[j]`

`i ++`

`j ++`

`i >= n`

`j >= n`

$$\{ x = y = i = j = 0 \}$$

`i < n`

`x += A[i]`

`j < n`

`y += A[j]`

`i++`

`j++`

`i >= n`

`j >= n`

$$\{ x = y \}$$

Generalization

 $\{ x = y = i = j = 0 \}$

generalization
across loop iterations
using interpolation

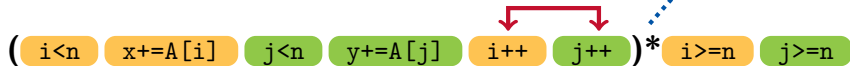
($i < n$ $x += A[i]$ $j < n$ $y += A[j]$ $i++$ $j++$) * $i \geq n$ $j \geq n$

 $\{ x = y \}$

Generalization

$\{ x = y = i = j = 0 \}$

generalization
across loop iterations
using interpolation

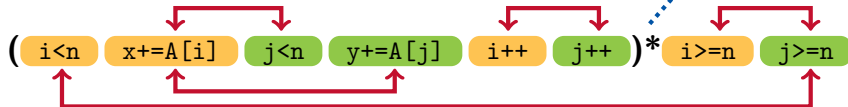


$\{ x = y \}$

Generalization

$$\{ x = y = i = j = 0 \}$$

generalization
across loop iterations
using interpolation

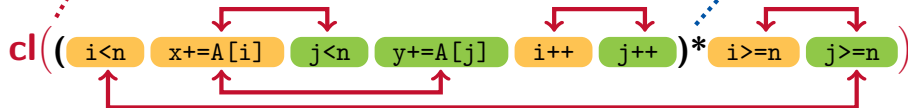

$$\{ x = y \}$$

Generalization

generalization
across interleavings
using commutativity

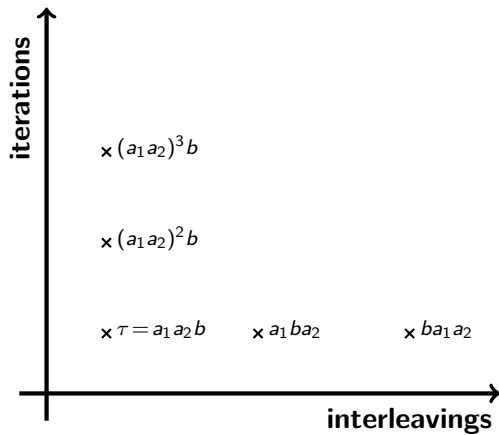
$$\{ x = y = i = j = 0 \}$$

generalization
across loop iterations
using interpolation

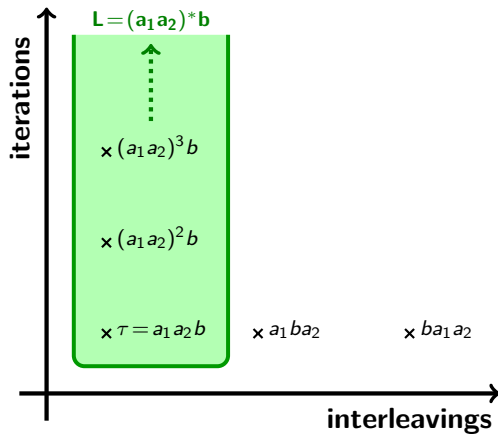


$$\{ x = y \}$$

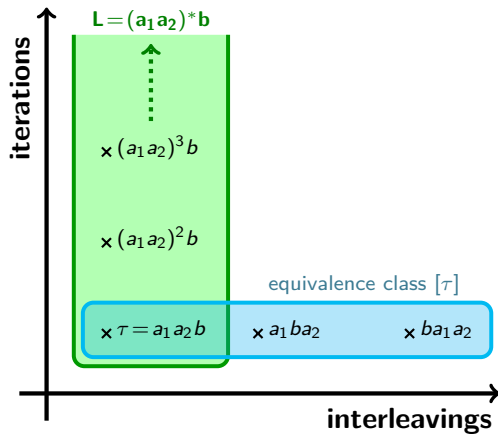
Generalization



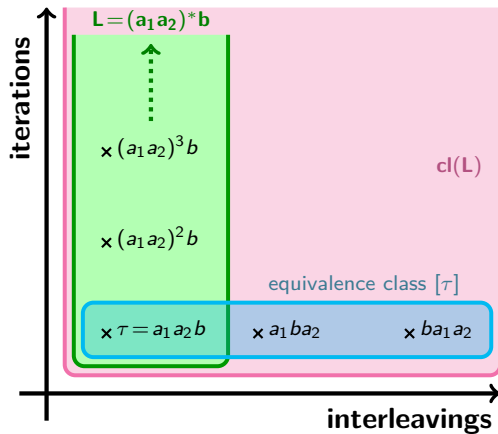
Generalization



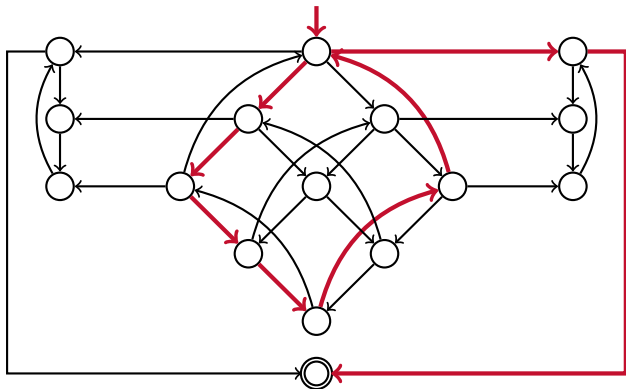
Generalization



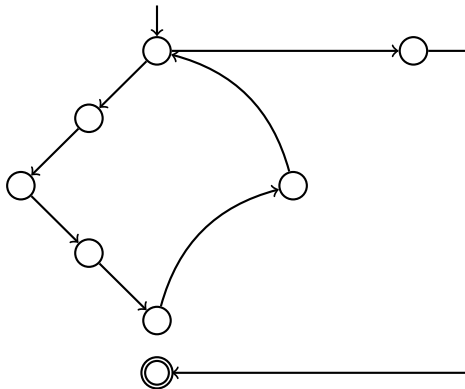
Generalization



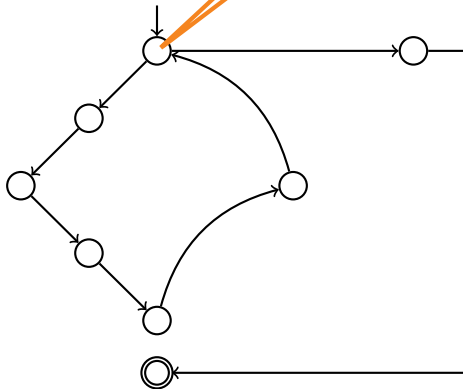
Key Idea



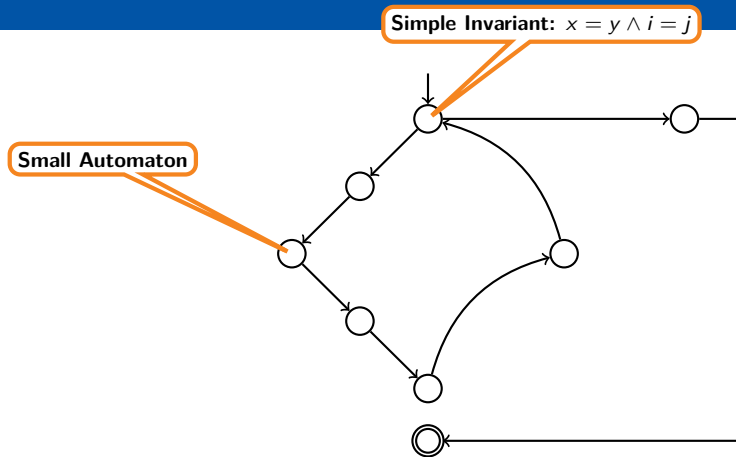
Key Idea



Simple Invariant: $x = y \wedge i = j$



Benefits



Ongoing & Future Work

- find more **commutativity**
- select the right **representatives**
- programs with **unbounded threads**

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- find more **commutativity**
- select the right **representatives**
- programs with **unbounded threads**

Find out more:

`ultimate-pa.org`

GemCutter poster at ETAPS

talk to me