

Adversarial Search for Gomoku

Gomoku, a deterministic strategy game, presents a huge challenge for adversarial search algorithms due to its

. The objective is to align five consecutive marks on an $n \times n$ grid (set to 9×9 in this report).

To address these challenges, four adversarial search algorithms were implemented:

1. **MinMax** : A baseline algorithm that explores all possible game states.
2. **AlphaBeta** : An optimized version of `MinMax`, pruning branches that can be confidently excluded based on the opponent's potential decisions.
3. **AlphaBetaHeuristic** : Enhances `AlphaBeta` by using heuristic evaluations to prioritize strategic moves.
4. **MCTS** : Leverages simulations for probabilistic decision-making, balancing real win probabilities with exploration.

The game board is a 9×9 grid implemented with a Python-based GUI using `tkinter`. `0` is denoted for User, `1` for computer.

1. MinMax :

- `minimax(board, depth, player)` : Explores all possible moves to determine the optimal outcome for the current player through exhaustive search.
- `minimax_helper(board, depth, player, alpha, beta)` :
 - `_maximize(current_depth, alpha, beta)` : Recursive function to maximize the score for the current player.

- **_minimize(current_depth, alpha, beta)** : Recursive function to minimize the score for the opponent.
- Note: `current_depth` and `alpha` parameters in `_minimize` are placeholders and are not used for pruning in this implementation.
- `minimax` : Computationally expensive due to exhaustive search, making it impractical for larger boards.
- `minimax` : Introduces a `max_depth` parameter to limit search depth and ensure reasonable response times. Without this, it would be infeasible to compute results, as the state space grows astronomically (e.g., $80! \approx 7.1569E+118$).

2. AlphaBeta :

- `alphabeta` : Improves `minimax` by eliminating branches that cannot influence the final decision.
- `alphabeta` :
 - **_apply_max_pruning(alpha, max_score, beta)** : Implements pruning for maximizing player.
 - **_apply_min_pruning(alpha, min_score, beta)** : Implements pruning for minimizing player.
- `alphabeta` : Reduces the search space significantly, enabling deeper exploration within the same time constraints.

3. AlphaBetaHeuristic :

- `alphabetaheuristic` : Extends `alphabeta` by integrating a heuristic evaluation function to estimate the desirability of intermediate board states.
- `alphabetaheuristic` :
 - Scores are assigned based on consecutive pieces and open ends (e.g., 4 consecutive pieces with 2 open ends are highly prioritized, followed by 4 consecutive pieces with 1 open end).
 - Penalizes the opponent's advantageous positions by blocking critical moves.
 - For detailed scoring logic, refer to the well-documented `HeuristicEvaluation` class.
- `alphabetaheuristic` :
 - **_calculate_heuristic_score(row, col)** : Computes the overall heuristic score for the current board state.
 - **_calculate_current_score(row, col, player)** : Assigns scores for the current player by evaluating their consecutives on the board.
 - **_calculate_opponent_score(row, col, opponent)** : Penalizes the opponent's consecutives by reducing the score for threatening positions.
 - **_evaluate_center(row, col)** : Adds a positional bonus for moves closer to the center of the board.

- : Enabling the AI to make more informed decisions within practical time constraints.

4. MCTS :

- : Leverages simulations to estimate the probability of winning from a given state. The algorithm follows four main steps:
 - a. (via `_Node.select()`): Traverses the tree using UCB1 to identify the most promising nodes for exploration.
 - b. (via `_Node.expand()`): Adds a new child node to the tree.
 - c. (via `_Node.simulate()`): Randomly simulates a game from the newly expanded node.
 - d. (via `_Node.back_propagate(winner)`): Updates the tree with simulation results.
- : A configurable time limit (default: 15 seconds per move) ensures the algorithm responds efficiently.
- :
 - `_Node.best_final_move` : Prioritizes moves that guarantee a win. If no such move exists, selects the most visited node to maximize the likelihood of success.

Experiments were conducted on a `max_depth`` and simulation counts to evaluate:

Following tests were conducted on a MacBook Pro M1 Pro chip (16GB).

1. MinMax :

- Depth-limited to due to exponential growth in game states.
- Struggles with longer simulations, making it easy for the user to win.
- On my Mac (), it expands approximately , but the AI consistently loses due to lack of strategic depth.

2. AlphaBeta :

- Runtime reduced by compared to through branch pruning.
 - At , results are produced in .
- Increasing

3. AlphaBetaHeuristic :

- Demonstrated improvements in AI' intelligent, effectively blocking user moves, prioritizing the center, and constructing consecutive pieces.
- On my Mac (), the first move takes , and subsequent moves take due to reduced board complexity. Performance improves significantly as the game progresses.

4. MCTS :

- Faces challenges in deterministic winning moves during endgame scenarios without fine-tuning .
- Fixed to (configurable). On my Mac, it performs approximately . The AI is significantly smarter, consistently blocking user moves and forming its own 5-consecutive pieces.

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| () | 11 | ~500,000 | Baseline for comparison |
| () | 0.2 | ~6,000 | Efficient pruning for deeper exploration |
| | 2 (average after 1st) | ~30,000 (average) | Strategic decisions, blocks, and center focus |
| | 15 | ~30,000 simulations | Adaptable probabilistic analysis, strategic wins |

: Win Rate (%) is influenced by the user's skill level. However, it is evident that the AI improves significantly in strategic decision-making with each algorithm upgrade.

- The Python package was used to handle the GUI. The initial GUI code was generated using ChatGPT-4 and subsequently modified and improved by me.
- All algorithm implementations, including , , , and , (single person in a group).
- This report was reviewed using ChatGPT to ensure proper English grammar and clarity.