

1. given x, y, z , penalty.
2. update x so that it is feasible for bounds and any linear constraints.
3. evaluate f, c, g, J and compute $\text{norm}_c, \text{max_infeas_bar}, \text{merit}$
4. $\text{iterate} = 0$, make sure blow-up is not signified
5. **BEGIN (main loop)**
6. compute residuals $C_RES_l, C_RES_u, A_RES_l, A_RES_u, X_RES_l, X_RES_u$.
7. IF $\text{iterate} = 0$ then check_optimal goto 9.
8. if x_k has moved then
 - if sqp used
 - if $\sim \text{bfgs}$
 - then compute J^{ya} from sqp
 - end
 - compute $A_t y_a$ from sqp and then check optimal
 - update $\text{primal_vl}, \text{dual_vl}, \text{comp_vl}$ and Y if necessary
 - end
 - if $\sim \text{bfgs}$
 - compute J_{ty} from cauchy
 - end
 - compute A_{ty} from cauchy and then check optimal
 - update $\text{primal_vl}, \text{dual_vl}, \text{comp_vl}$ and Y if necessary
- else
 - if sqp computed
 - compute J_{ty} and A_{ty} and then check optimal
 - update $\text{primal_vl}, \text{dual_vl}, \text{comp_vl}$ and Y if necessary
 - end
 - compute A_{ty} and J_{ty} from cauchy and then check optimal
 - update $\text{primal_vl}, \text{dual_vl}, \text{comp_vl}$ and Y if necessary
 - end
9. If optimal or $\text{iterate} = \text{max_iterate}$, go to 13.
10. check subproblem optimal based on point accepted in 8, which is same as in $\text{nlp}\%Y$
11. determine whether to increase penalty parameter (if blowup, subproblem optimal, other?)
12. evaluate merit function if penalty parameter has changed
13. print : $\text{iterate}, \text{primal_vl}, \text{dual_vl}, \text{comp_vl}, \text{penalty parameter}, \text{merit}$
14. if optimal or $\text{iterate} = \text{max_iterate}$, EXIT
15. $\text{iterate} = \text{iterate} + 1$
16. IF BFGS then update $B(s_f \text{ or } s_c, \text{grad}Lx, \text{grad}Lx_{\text{new}}, B)$ note: make sure update knows when it is first iterate so that it can handle first iterate.
17. compute predictor step/mults
18. Evaluate H possibly at Cauchy mults.
19. compute cauchy step/mults and model decrease
20. possibly compute sqp step/sqp mults and model decrease at full step
21. IF sqp not computed OR sqp computed but not good then eval. $f_{\text{new}}, c_{\text{new}}$ at Cauchy pt.
ELSE evaluate $f_{\text{new}}, c_{\text{new}}$ at sqp step.
22. IF blow-up, then signify.
23. compute ratio
24. print : (on separate line) everything to do with predictor, cauchy, and sqp : TR
25. IF “blow up” then decrease trust-region
ELSE if success, then
 1. update trust-region

2. compute $\text{gradLx}(g, J, Y)$ where Y corresponds to whether cauchy or sqp step was used
3. $x \leftarrow x_{\text{new}}$ (depends on whether SQP was used), $c \leftarrow c_{\text{new}}$, $f \leftarrow f_{\text{new}}$, $\text{norm}_c = \text{norm}_{c_{\text{new}}}$
4. update merit
5. evaluate $g \leftarrow g_{\text{new}}$, $J \leftarrow J_{\text{new}}$
6. compute $\text{gradLxnext}(g, J, Y)$ where is same Y from 24.2.
ELSE failure, then update trust-region.

26. END (main loop)